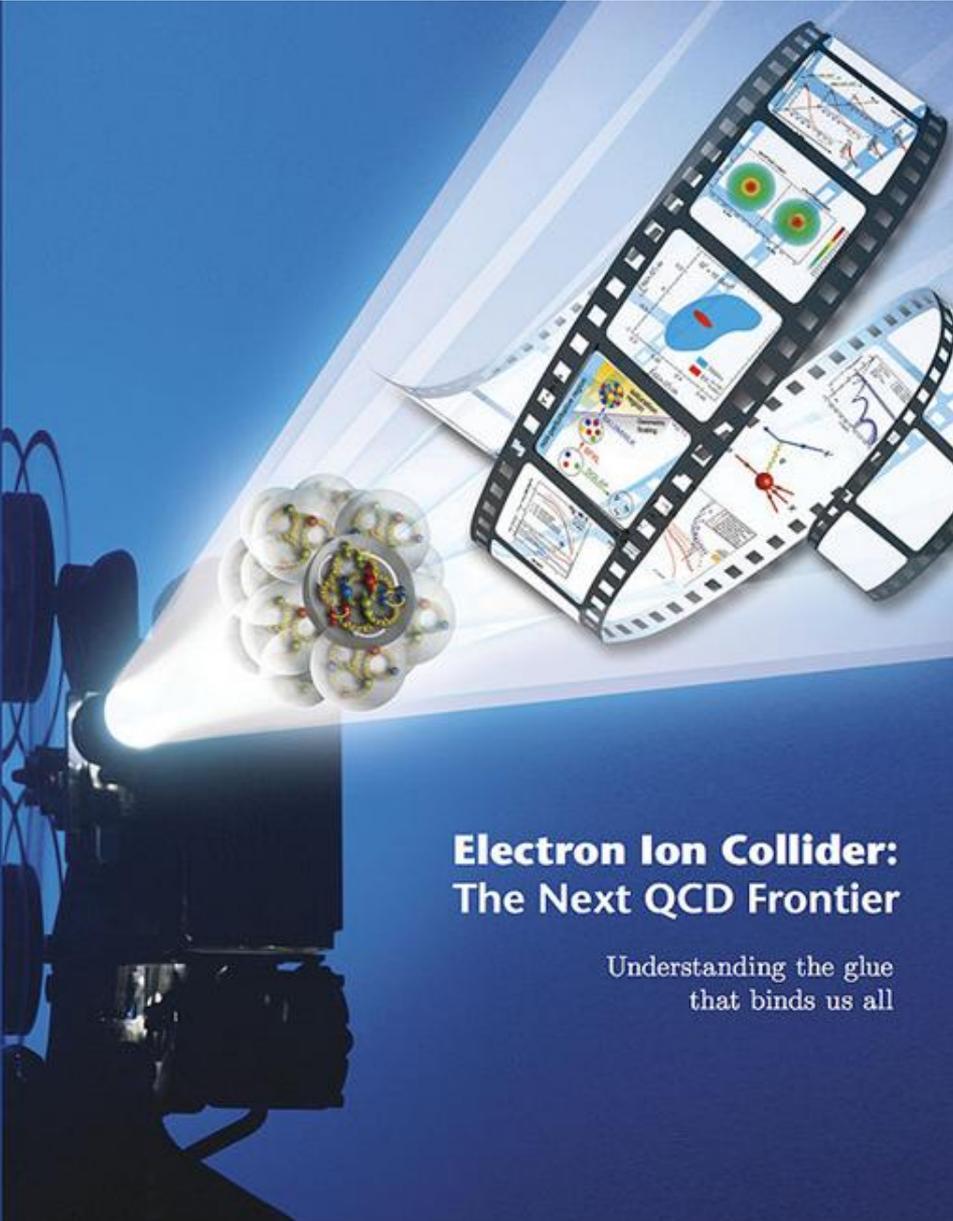


Detectors for an Electron Ion Collider

Thomas K Hemmick
Stony Brook University

- ▶ RHIC future is viewed by most to center on an “Electron–Ion Collider”
- ▶ R&D underway ~few yrs.
- ▶ Consortia:
 - Tracking/RICH
 - SBU, BNL, Yale, U Va, FI Tech.
 - Calorimetry



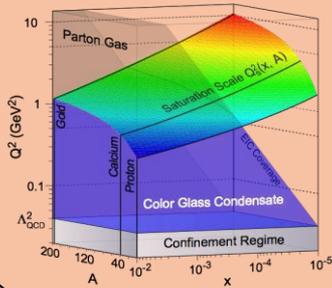
**Electron Ion Collider:
The Next QCD Frontier**

Understanding the glue
that binds us all

**Today: Overview of
“Tracking Consortium”
with emphasis on RICH**

Most Compelling EIC SCIENCE Questions

Where does the saturation of gluon densities set in?



Is there a simple boundary that separates the region from the more dilute quark gluon matter? If so how do the distributions of quarks and gluons change as one crosses the boundary?



Does this saturation produce matter of universal properties in the nucleon and all nuclei viewed at nearly the speed of light?

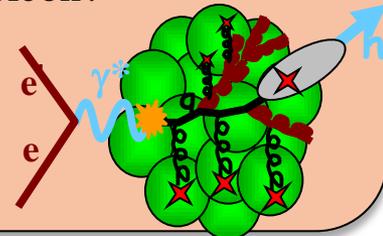
How does the nuclear environment affect the distribution of quarks and gluons and their interaction in nuclei?



How does the transverse spatial distribution of gluons compare to that in the nucleon?

How does matter respond to fast moving color charge passing through it?

Is this response different for light and heavy quarks?



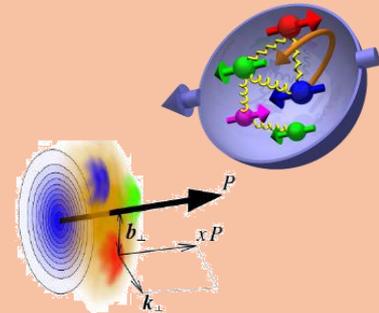
How are sea quarks and gluons and their spin distributed in space and momentum inside the nucleon?



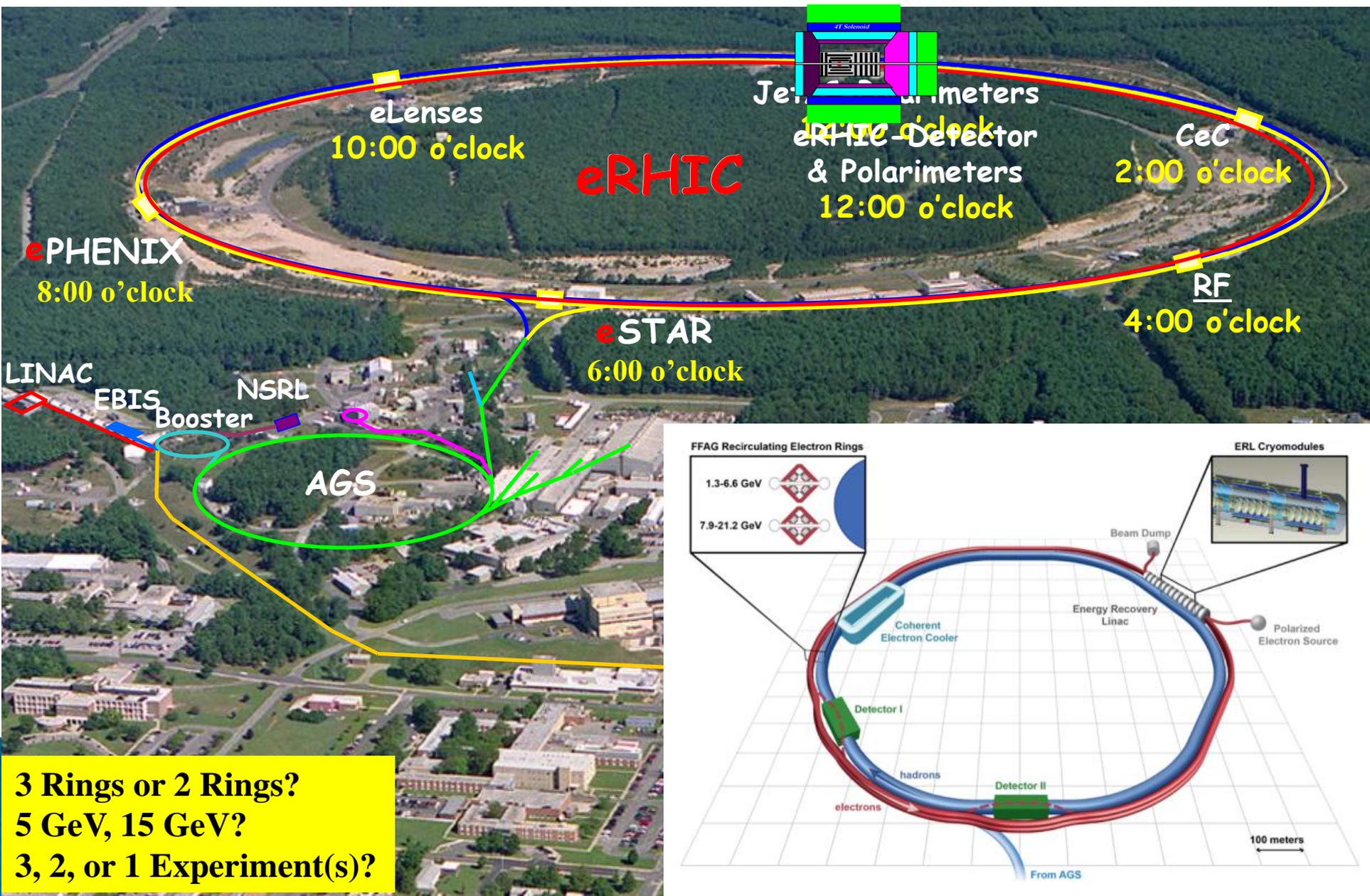
How are these quark and gluon distributions correlated with the over all nucleon properties, such as spin direction?



What is the role of the motion of sea quarks and gluons in building the nucleon spin?

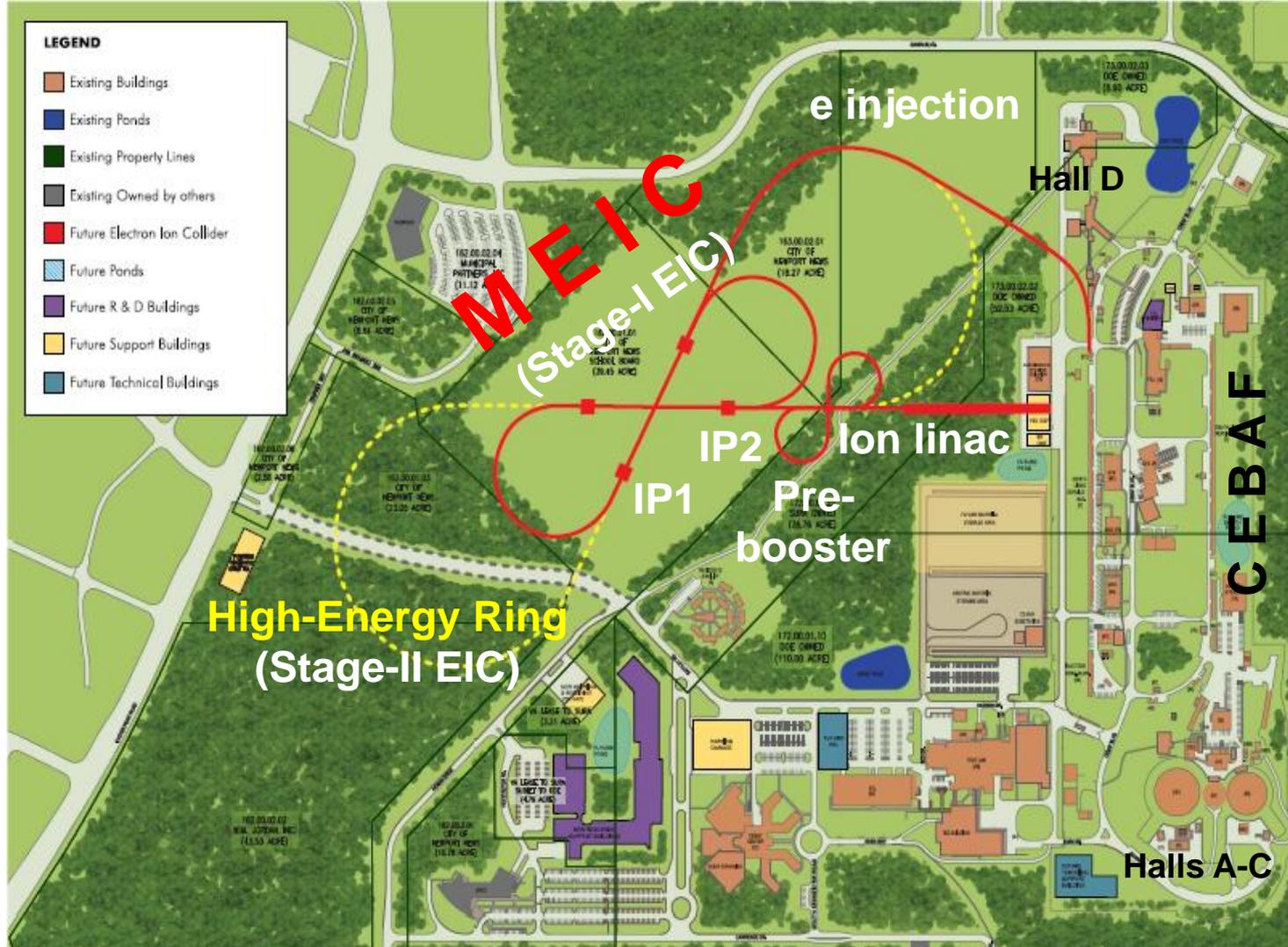


From RHIC to eRHIC



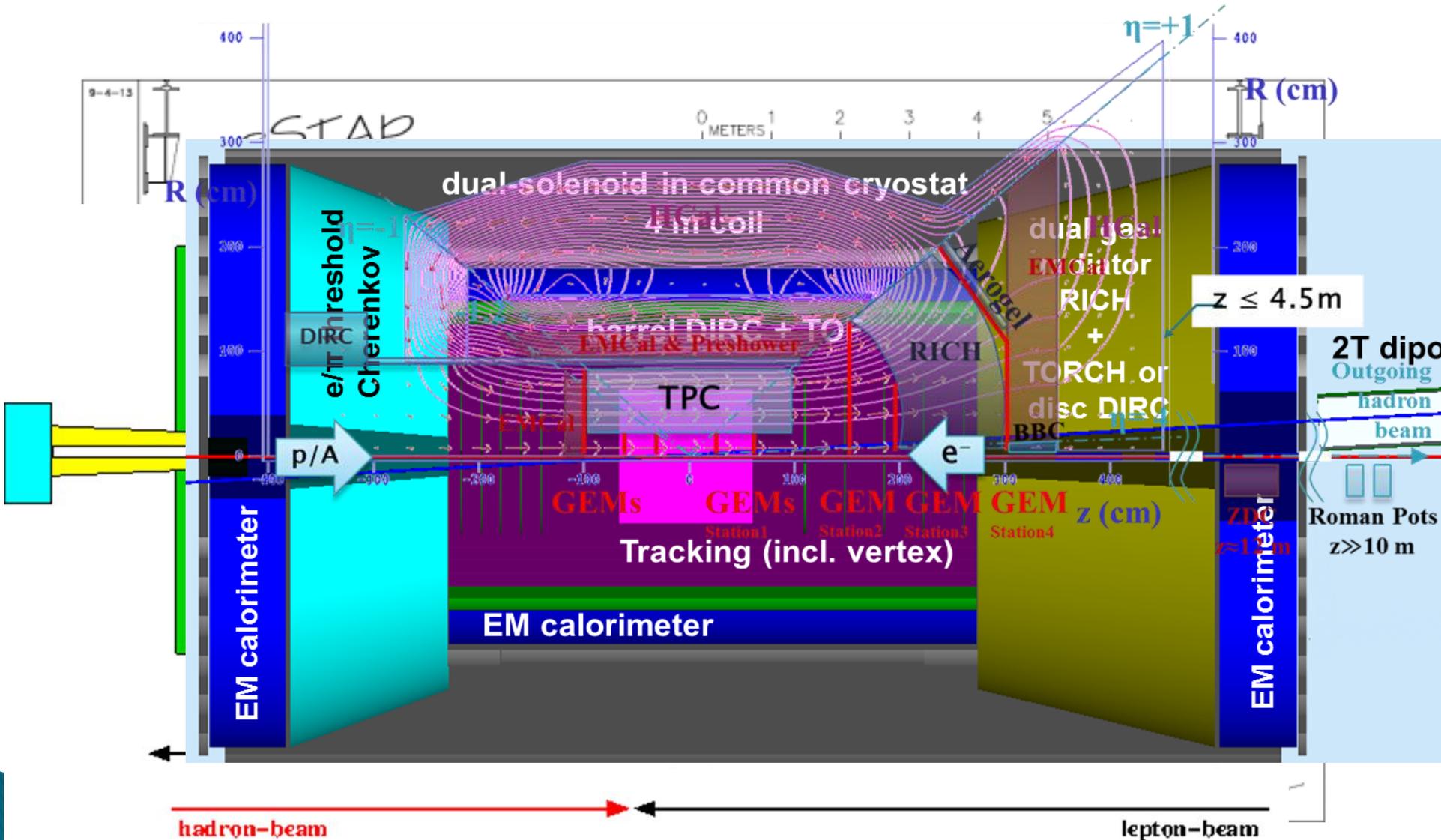
3 Rings or 2 Rings?
 5 GeV, 15 GeV?
 3, 2, or 1 Experiment(s)?

The EIC at Jefferson Lab



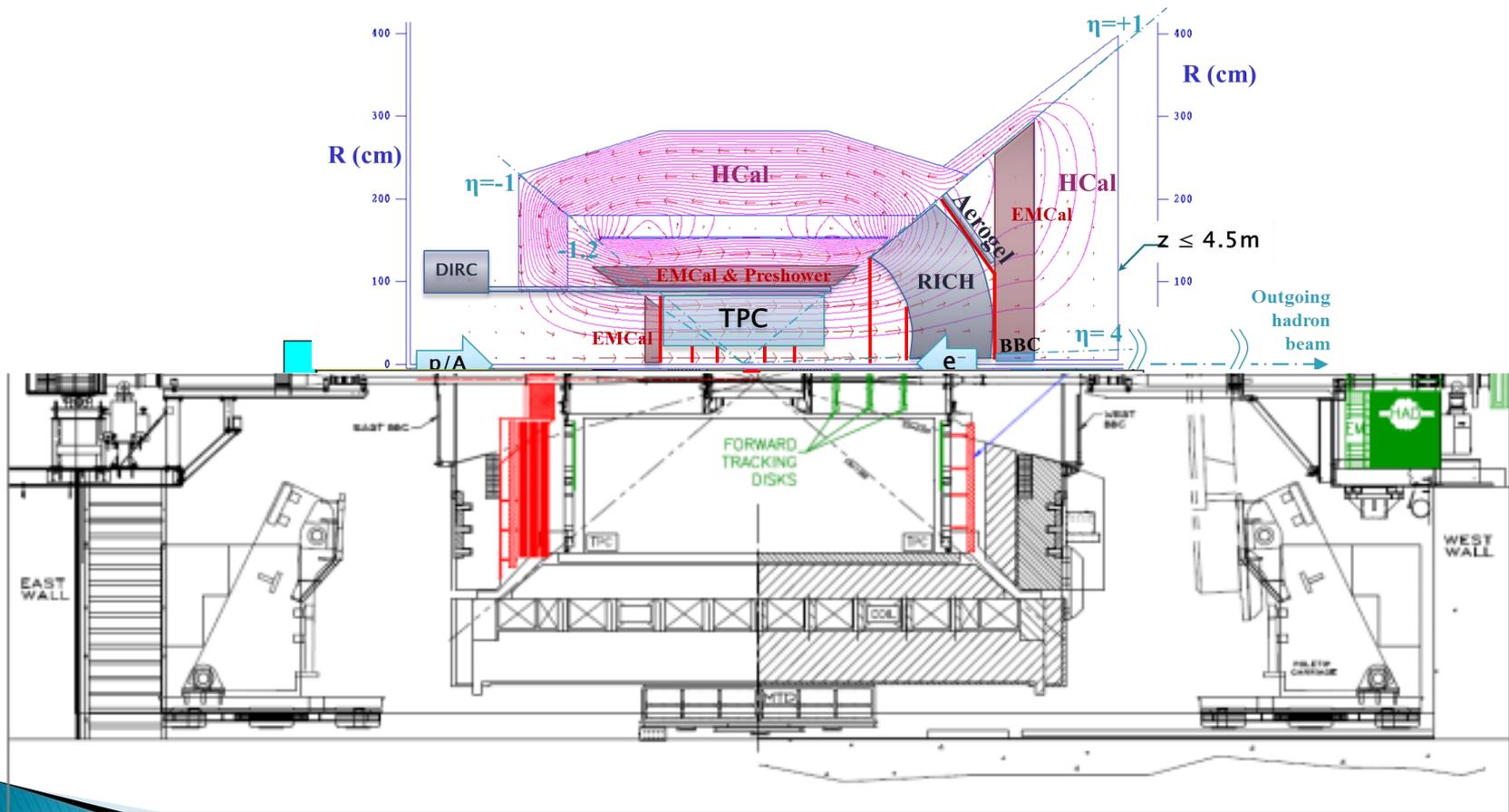
- The MEIC has a circumference similar to CEBAF (1.4 km)

Four Detector Designs



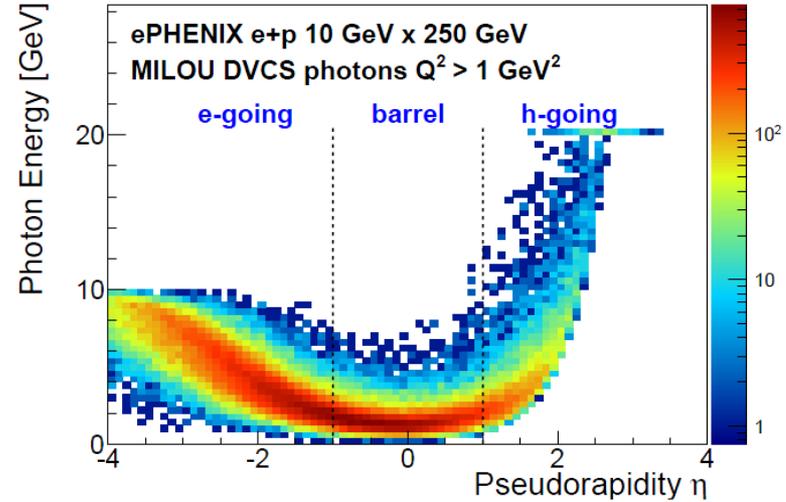
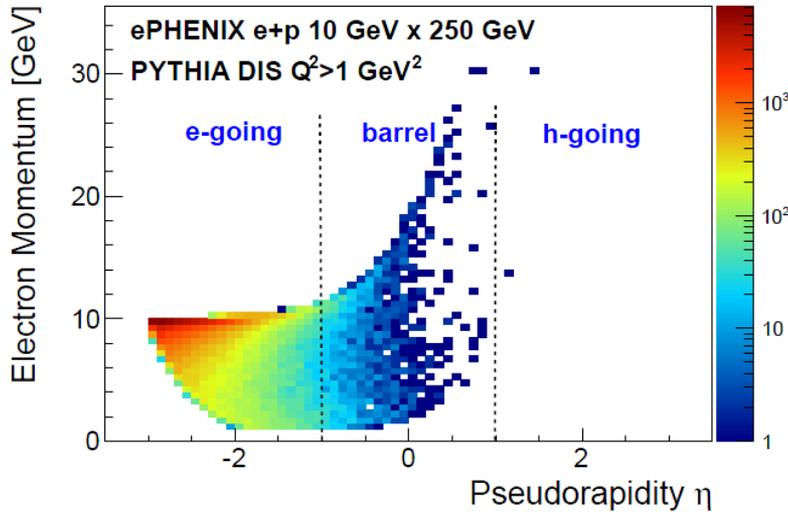
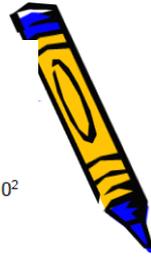
Most designs favor TPC for central tracking due to low momentum PID and low mass

Detector Designs - to scale

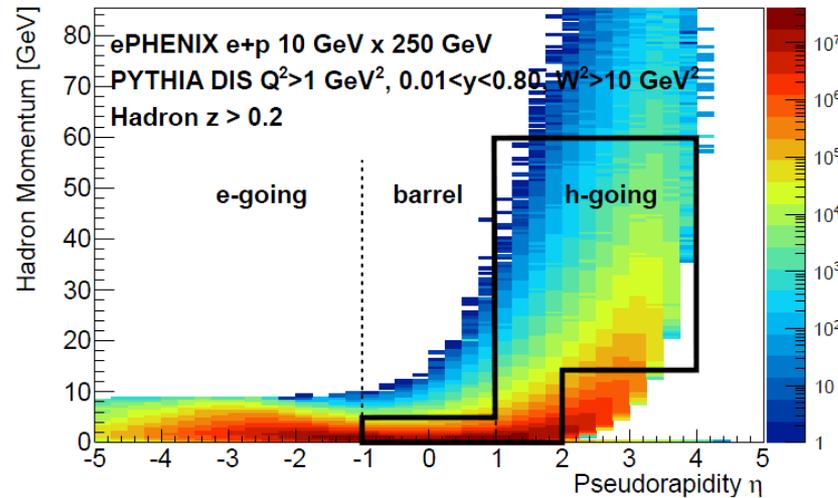




Measure what comes out!



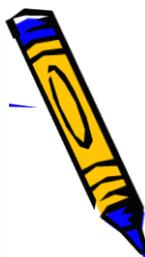
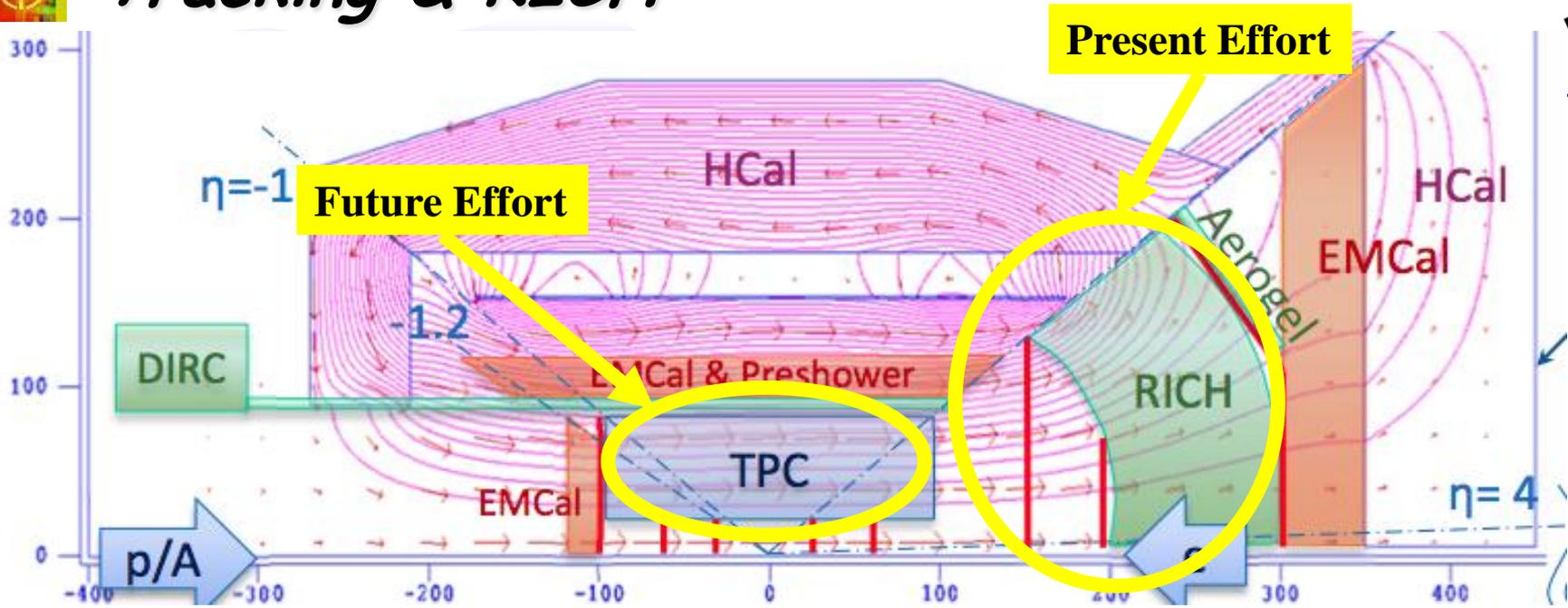
- ❑ ep (eA) **HIGHLY** asymmetric.
- ❑ Moderate momenta for **ALL** species mid- and negative- η .
- ❑ At mid-rapidity principally low momentum:
 - **dE/dx** at lowest p.
 - **DIRC** to extend to **~8 GeV**
- ❑ Fwd η **BIG** challenge
 - **Hadron ID** req'd to **60 GeV/c!!**



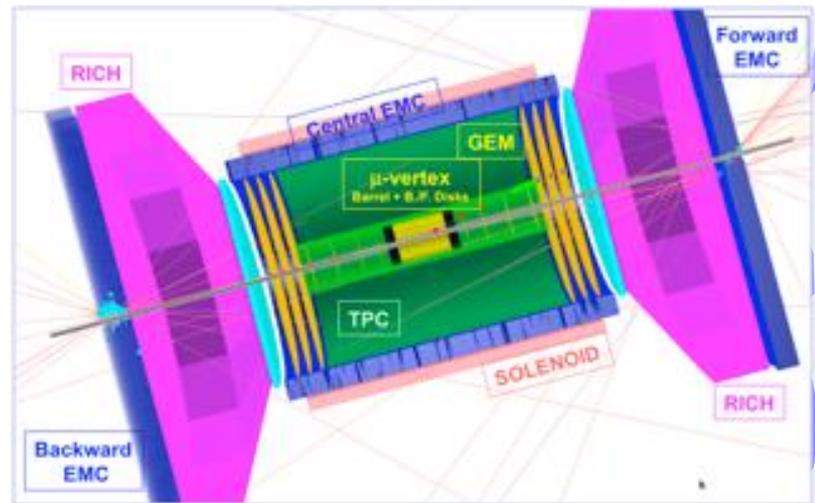
Ring Imaging Cherenkov is only known technology with required momentum reach!



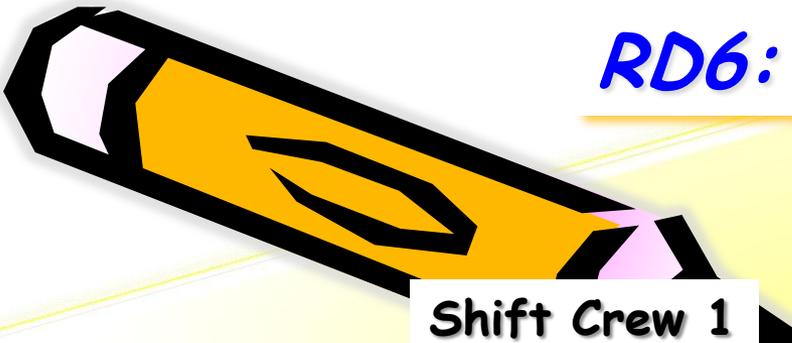
Tracking & RICH



- ❑ "Forward" region requires:
 - Planar tracking chambers.
 - High Momentum PID Device.
- ❑ Prototypes placed in test beam address issues for:
 - Planar GEM-based trackers.
 - Ring-Imaging Cherenkov (RICH)
- ❑ Future has TPC!



RD6: Tracking/PID Consortium



Shift Crew 1



Shift Crew 2



Test Beam Oct 2014:
BNL
Florida Tech
Stony Brook University
Thomas Jefferson Lab
University of Virginia
Yale University

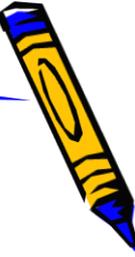
New members (TPC)
LLNL, WIS, LBNL



Note: Photo shows Beam Shifters only!



Principle Focus of "Consortium" Research



□ End-Cap R&D (subject of test beam)

➤ Mini-drift GEM chambers:

Ⓞ BNL; overcomes degradation of resolution with angle.

➤ 3 Coordinate Readout:

Ⓞ Yale; X-Y-U match charge & geometry to reduce channel counts

➤ Large GEM chambers:

Ⓞ UVA; Small angle stereo chamber "Compass Style"

Ⓞ FIT; Zig-zag & Stretched foils eliminates spacers.

➤ Compact RICH:

Ⓞ SBU; CsI/GEM & dielectric mirror reduces radiation 3m→1m

□ Barrel R&D (upcoming)

➤ TPC with HBD

Ⓞ BNL, SBU, Yale

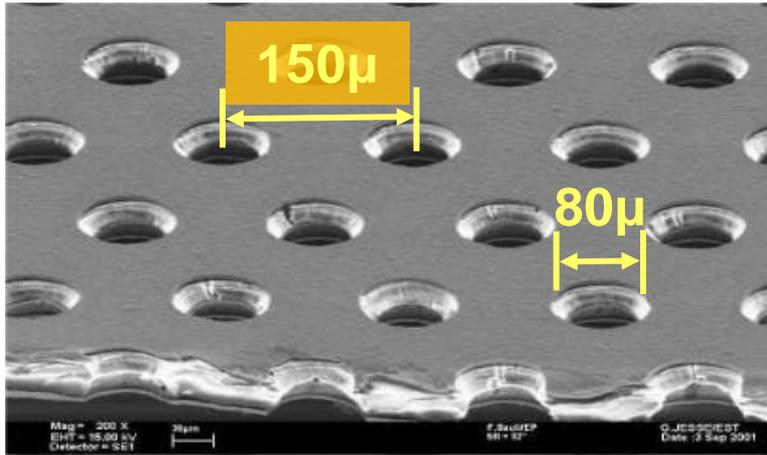
➤ **New this year: Large TPC (LLNL, WIS).**



Common Technology: Gas-Electron Multiplier (GEM)

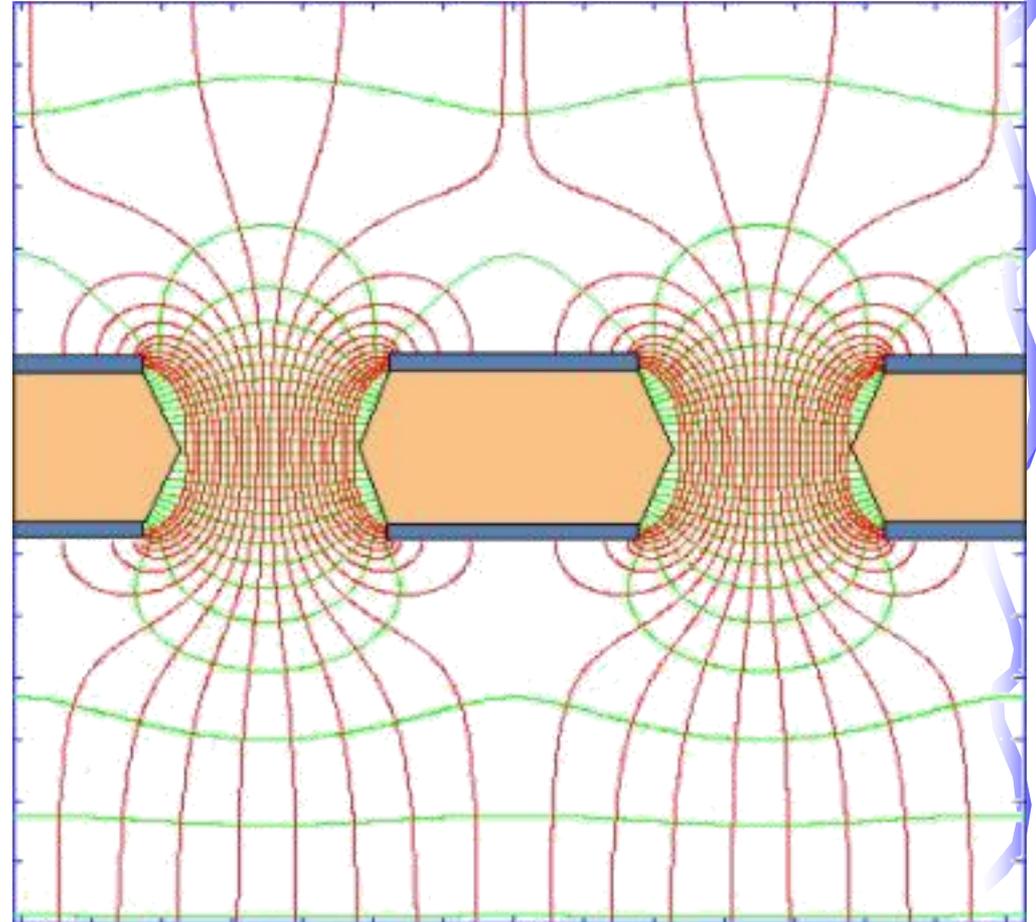


Gas Electron Multiplier for PHOTONS!



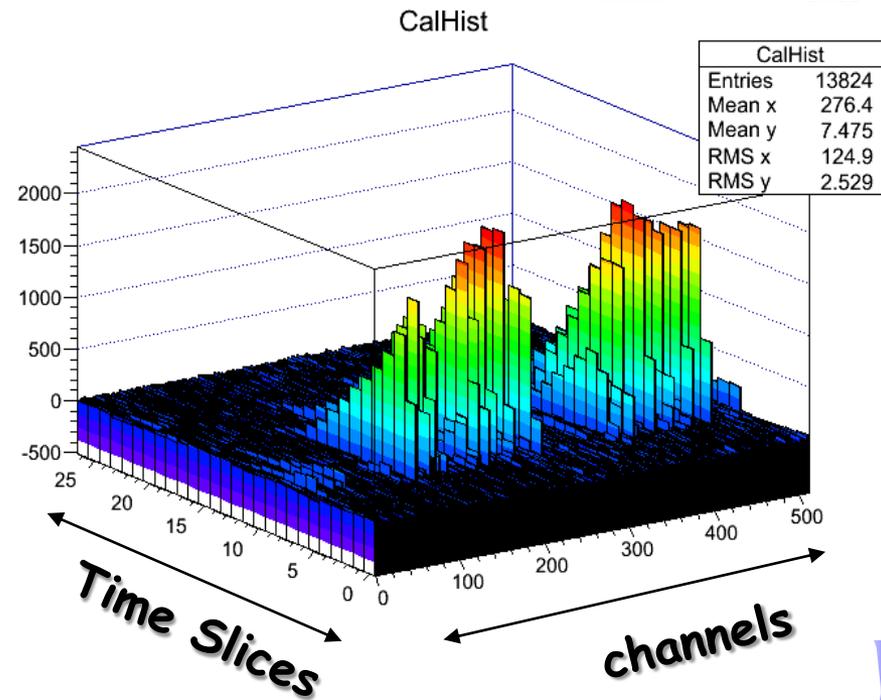
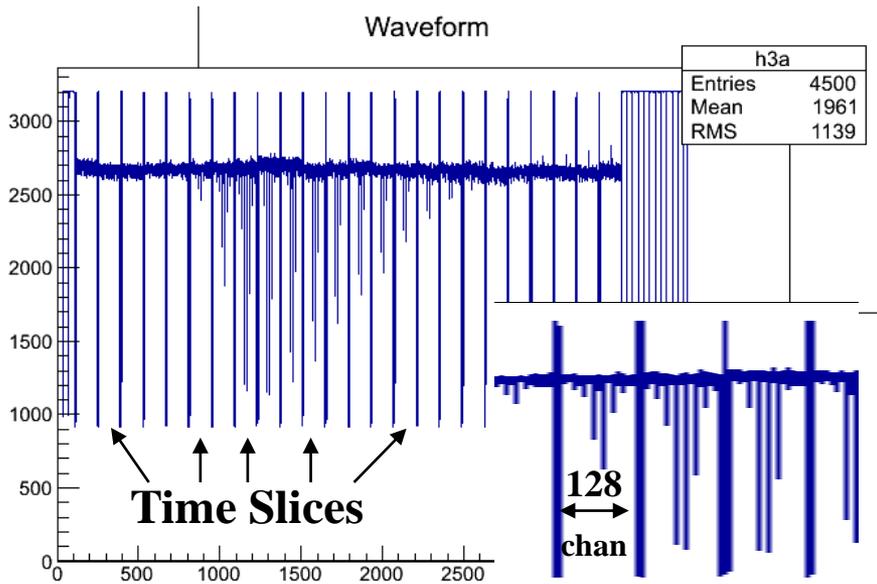
- ❑ The original idea by F.Sauli (mid 90s) US Patent 6,011,265
- ❑ Traditionally CHARGED PARTICLE detectors (not photons)

- ❑ Two copper layers separated by insulating film with regular pitch of holes.
- ❑ HV creates very strong field such that the avalanche develops inside the holes
- ❑ Multiple devices can be stacked to increase gain.

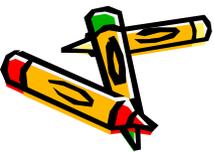




SRS Readout for Test Beam (inexpensive)



- ❑ APV25 chip:
CMS;128-chan Analog pipeline
- ❑ Flash digitized, read through Gbit Ethernet to PC.
- ❑ 2048 chan system ~5000 chf

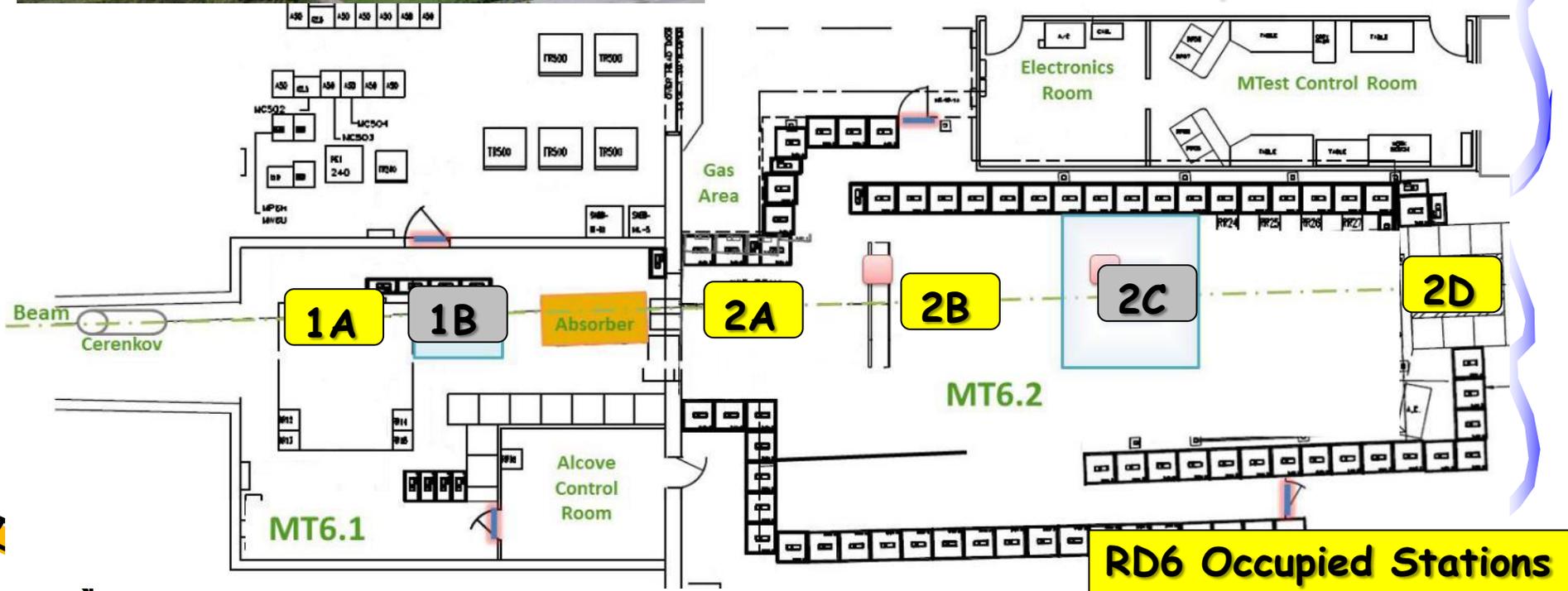
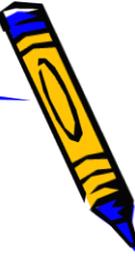




Fermilab Test Beam Facility

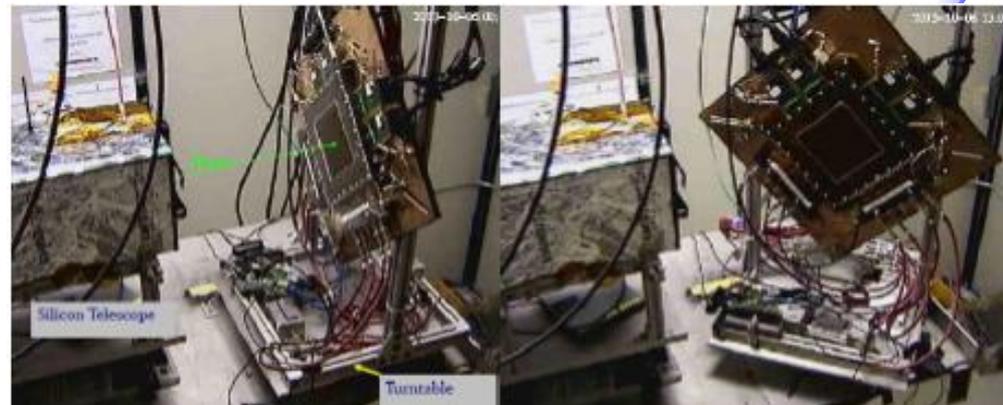
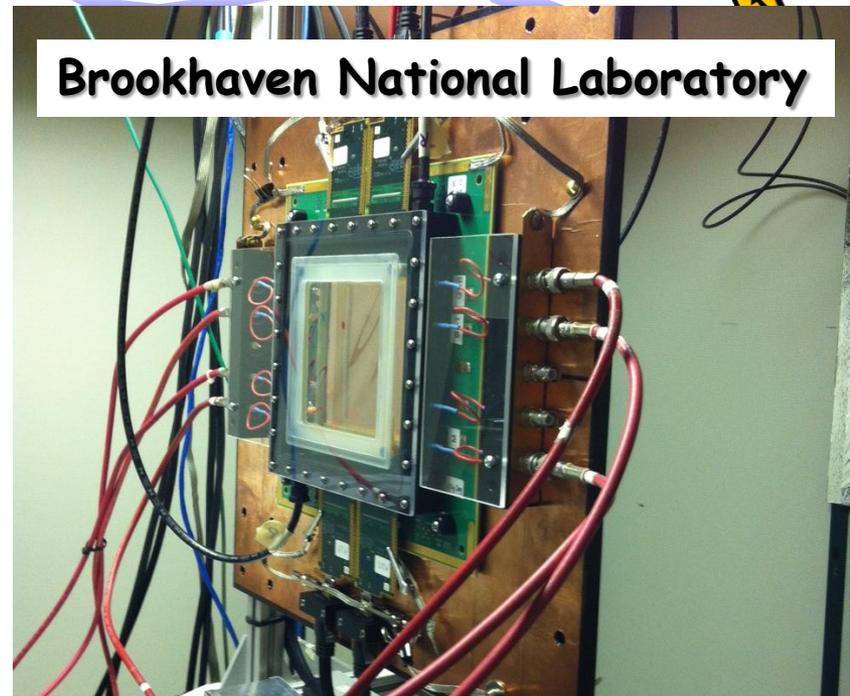
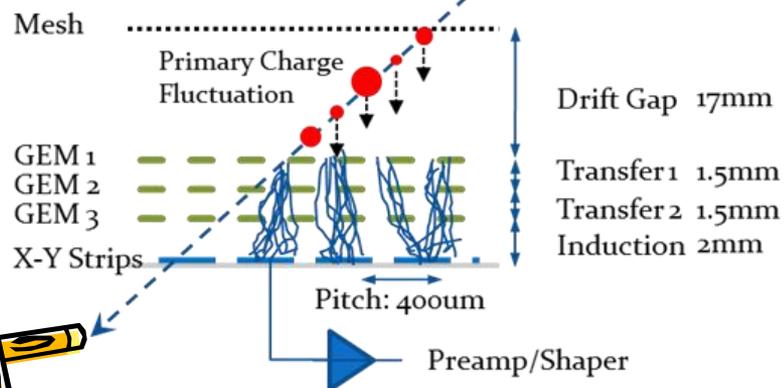


- ❑ "Meson Hall" repurposed.
- ❑ Beam(s)
 - 120 GeV protons (primary)
 - 1-32 GeV π Kp (ds-target)
 - 8-66 GeV π (us-target)
- ❑ 4 sec spill once per minute.
 - 10,000 counts/spill



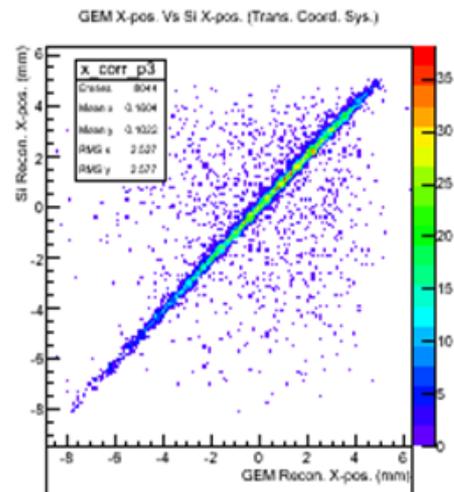
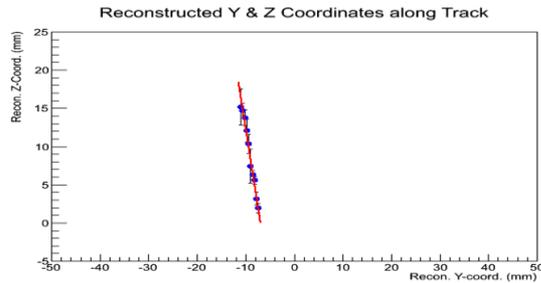
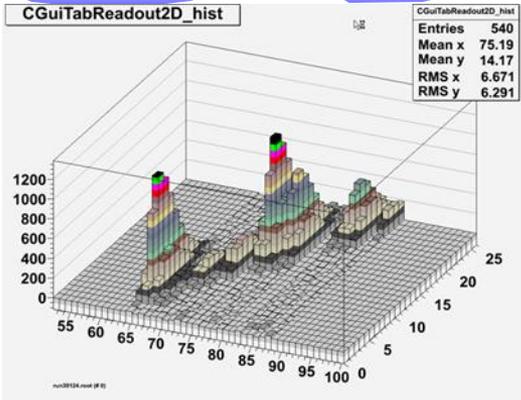
MT6 1A - Minidrift GEM chamber

- Challenge: Standard GEM tracking chambers have their resolution deteriorate with non-normal incidence.
- Approach: Raising the grid above the first GEM allows each chamber to measure a vector to correct for the inclination of every track.

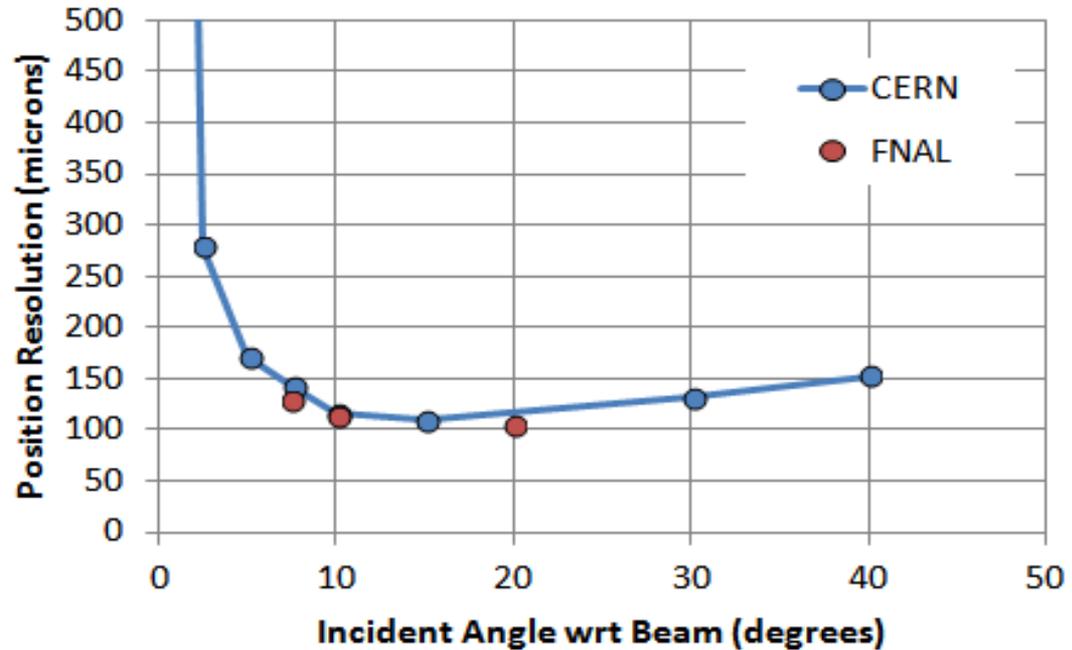




MT6 1A: Mini-Drift Principle Works.

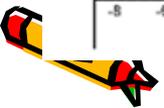


Mini-drift GEM Tracker Position Resolution Vs Angle
[Equal-Components, Det. Eff ~100%]



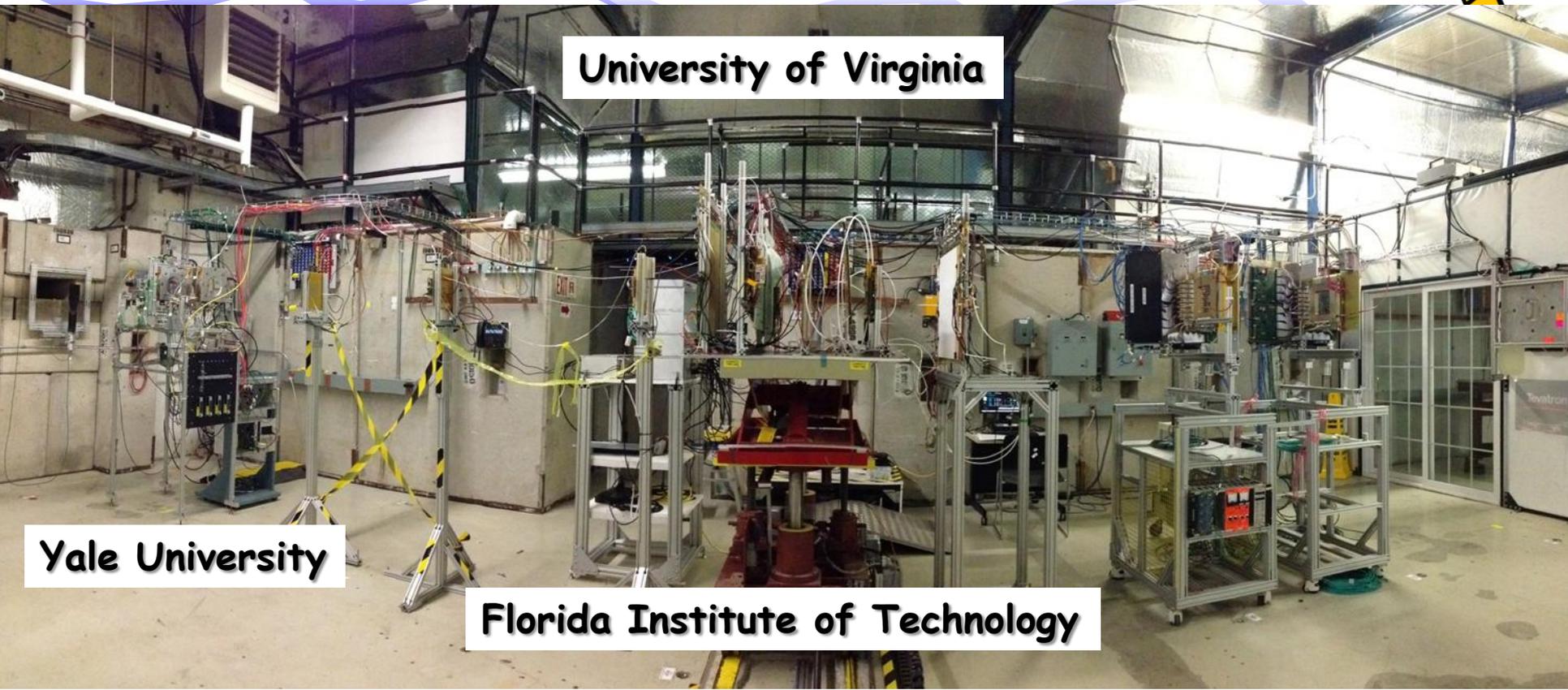
- CERN: Resolution limited by Reference.
- FNAL uses Silicon Tracker Reference.
- FNAL @ 20° = 104 μm (vs 118 μm)!

NOTE: Mini-Drift can be added to any chamber.





MT6 2A and 2B



University of Virginia

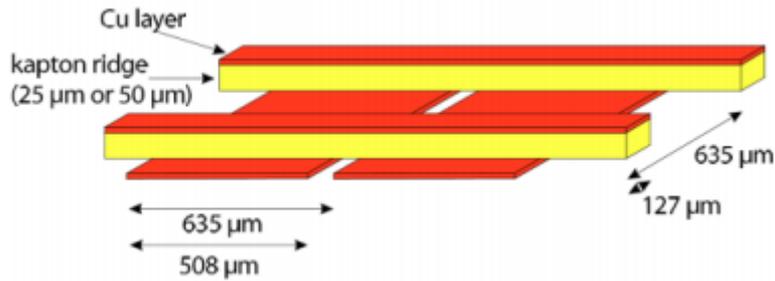
Yale University

Florida Institute of Technology

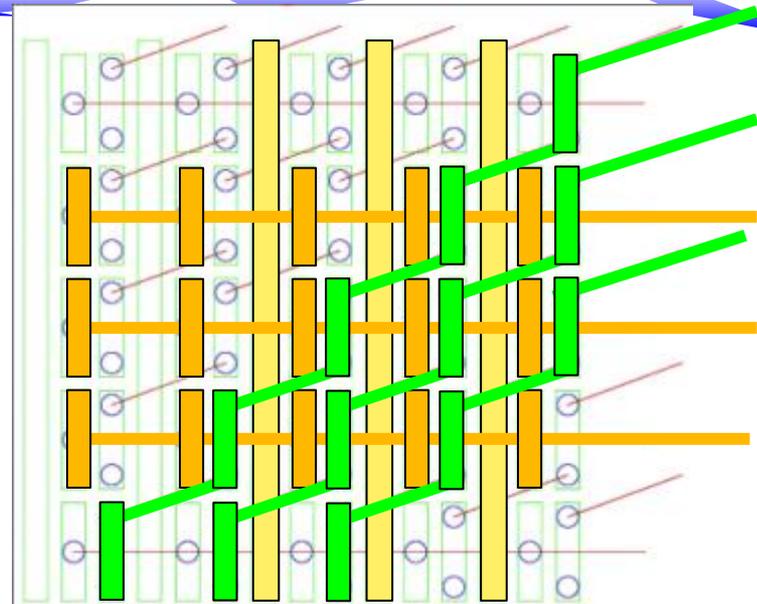
- ❑ Extensive setup of trackers at station 2B
- ❑ Testing new readout schemes.
- ❑ Testing largest area GEM detectors built in the US.



MT6-2A 3-coordinate readout



Standard Cartesian Readout
- "Compass Style"
- XY Hit Matching by Charge

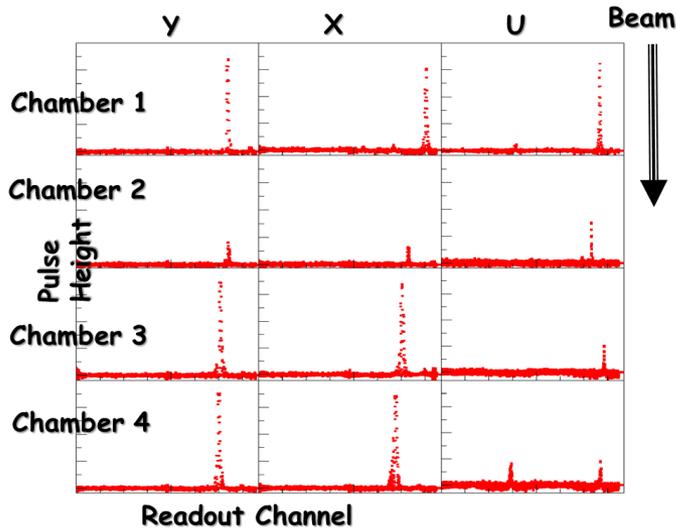


New 3-coordinate Readout
-Hit matching: **GEOMETRY & CHARGE**

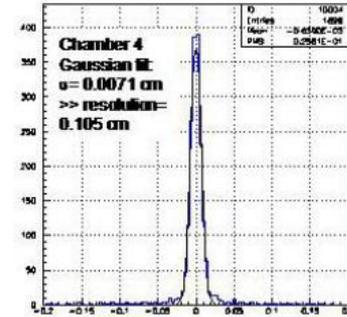
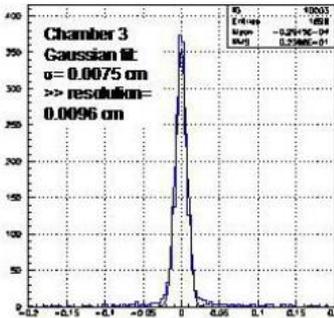
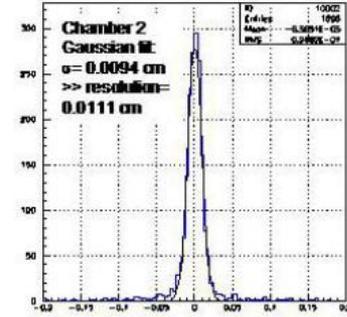
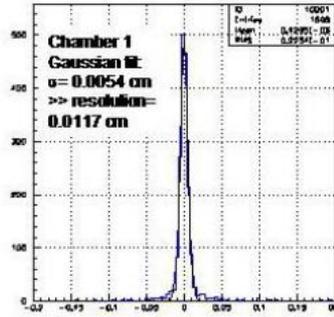
- Challenge:
Cartesian Readouts can lead to ambiguities in X-Y associations for high multiplicity events.
- Solution:
3 coordinate readout made on double-sided kapton.
- Goal:
Increased tracks per "patch" reduces channel count.



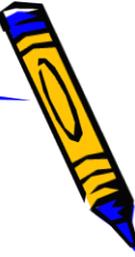
MT6 2A



- ❑ Event display - four single plane 3-coordinate GEM Chambers
- ❑ Single track fires x,u,y in all planes.

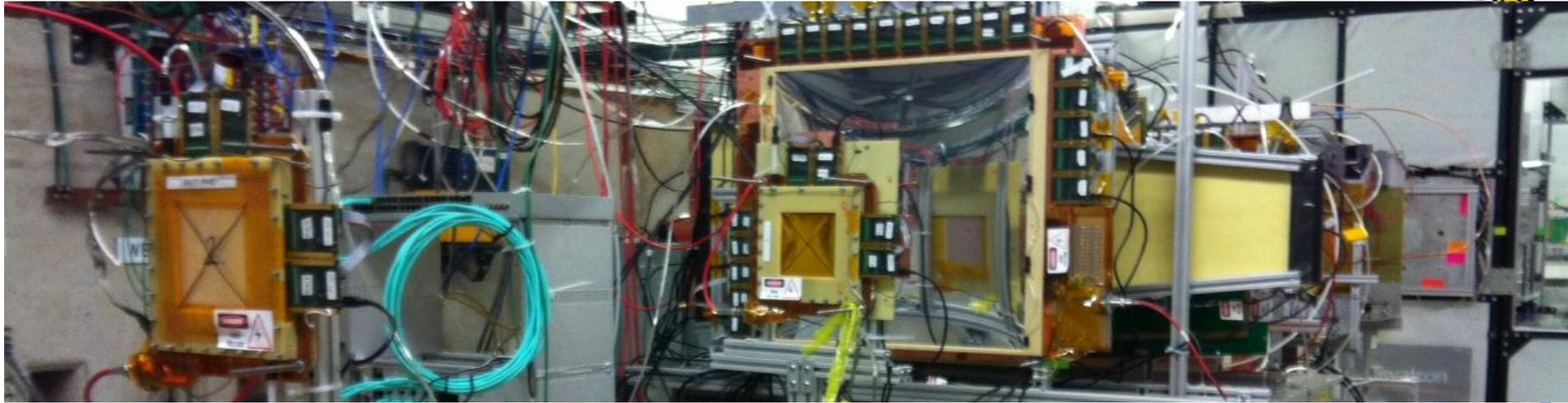


- ❑ X-residuals in four chambers.
- ❑ Resolutions from 97-117 μm .
- ❑ Result is **superb** since the readout pitch is coarse.
- ❑ Further analysis to determine maximum hits per region.





MT6 - 2B Large Area Tracking Chambers



□ Challenge:

GEM detector technology must be expanded in size to be useful in large experiments. Other than at CERN, these are the largest area GEM trackers in the world.

□ Furthermore:

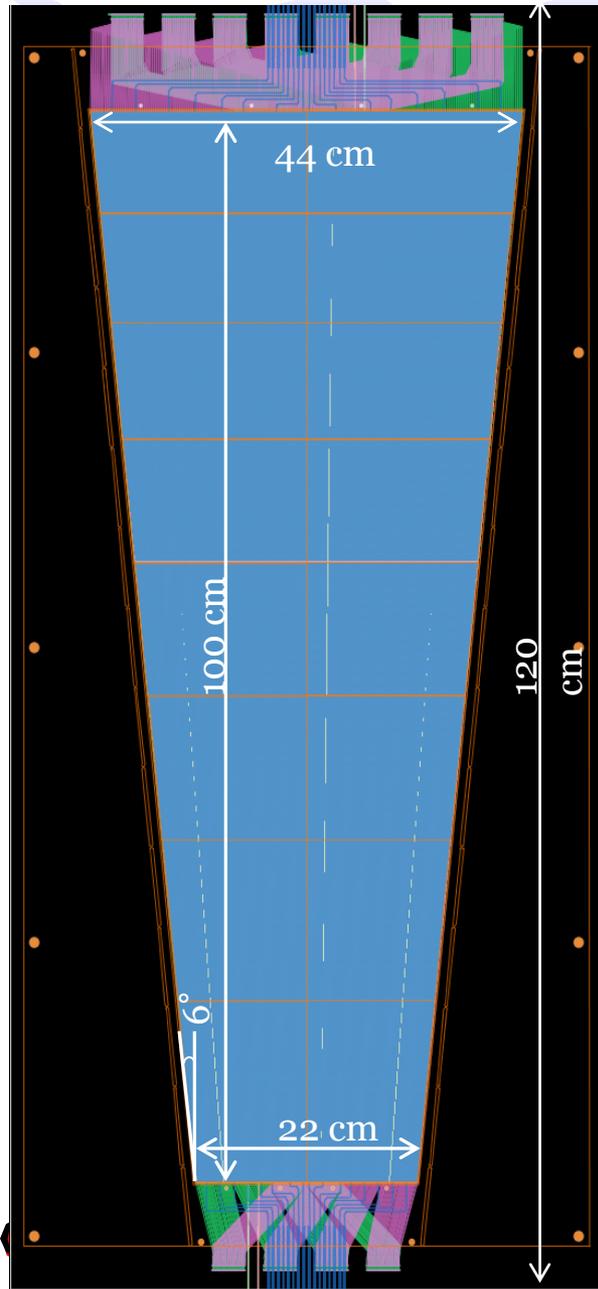
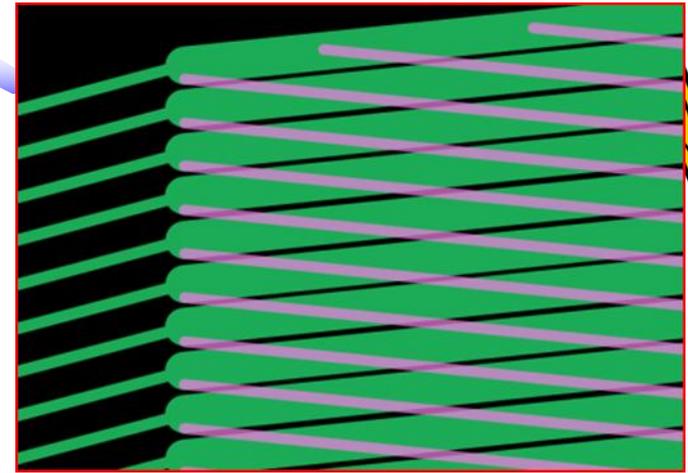
Alternative Readout using ZigZags & "Stereo-Compass"





“Stereo Compass”

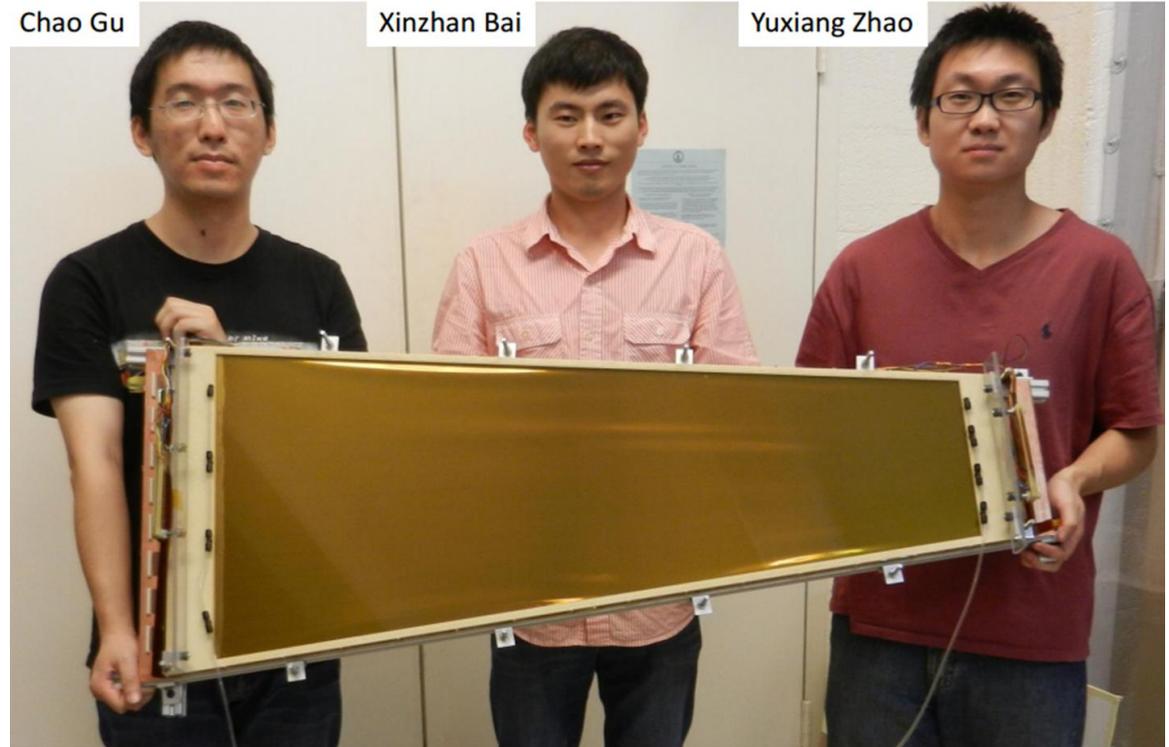
- Strips @ 12° stereo
- Full-sized for EIC.
- Largest “Compass-style” ever produced.



Chao Gu

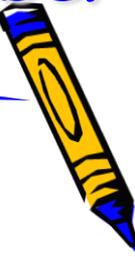
Xinzhan Bai

Yuxiang Zhao





Some Results on Large Compass-Style Chamber



Scan Beam Spot

Charge Match

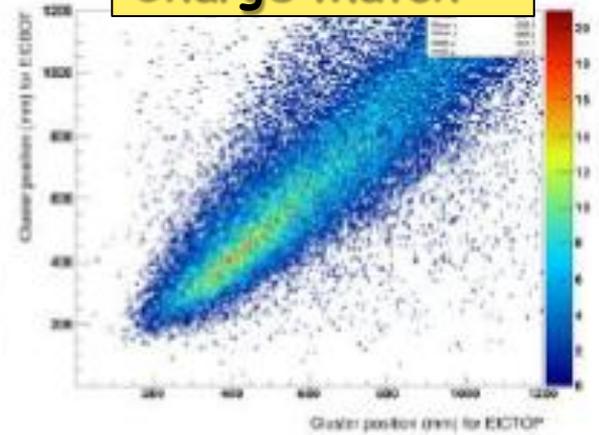
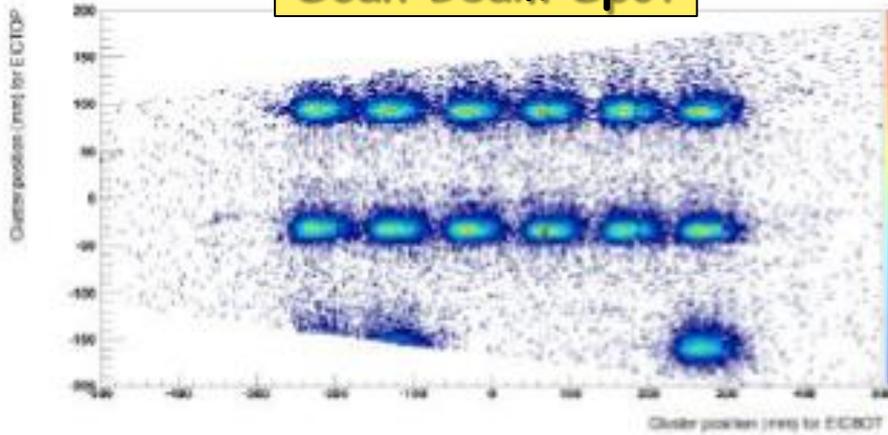


Figure 29: 25 GeV Hadron beam position scan (left); u-v strips charge sharing correlation (right).

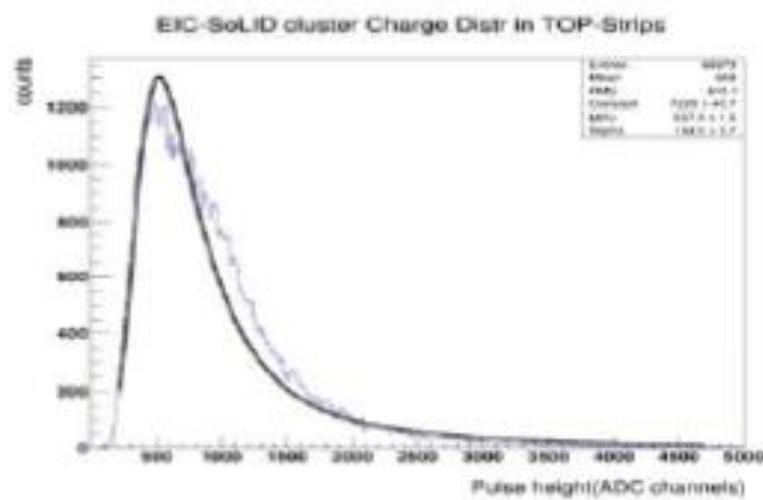
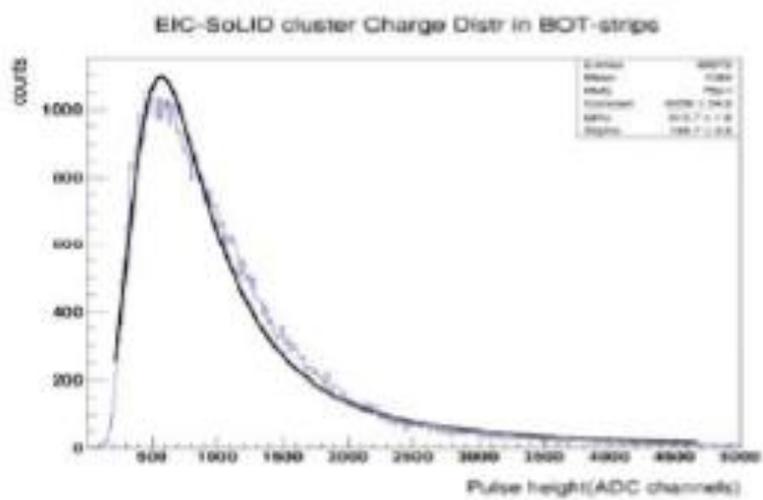


Figure 30: cluster charges distribution with Landau fit on v-strips (left) and u-strips (right).



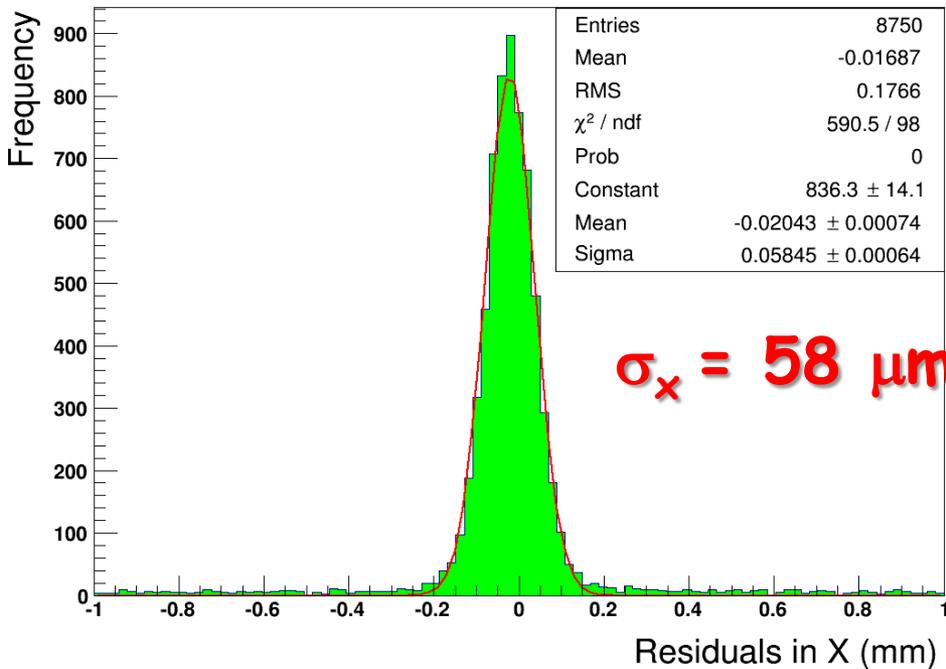


Spatial Resolution of SBS1

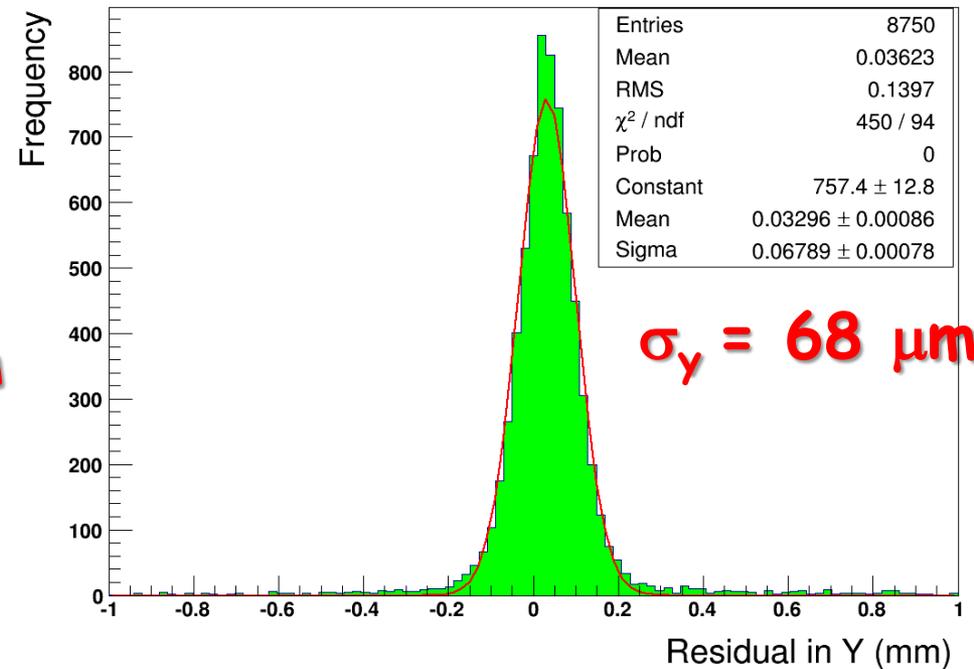


- **Combined distribution** : Exclusive and Inclusive residual distribution are merged
- **Resolution**: Width ($\sigma_{\text{resolution}}$) of the Gaussian fit to the combined residual distribution
- **Resolution**: $\sigma_{\text{resolution}} = \text{sqrt}(\sigma_{\text{exclusive}} \times \sigma_{\text{inclusive}})$

SBS1 X-Strips Spatial Resolution

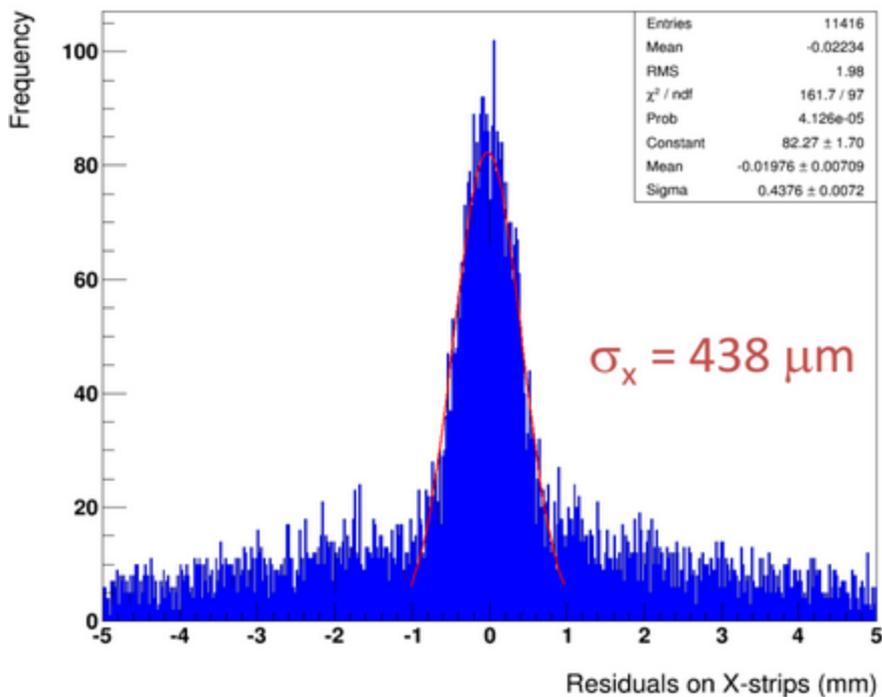


SBS1 Y-Strips Spatial Resolution



120 GeV Proton: Residuals of the EIC-SoLID with 430 mm

EIC1X Residuals

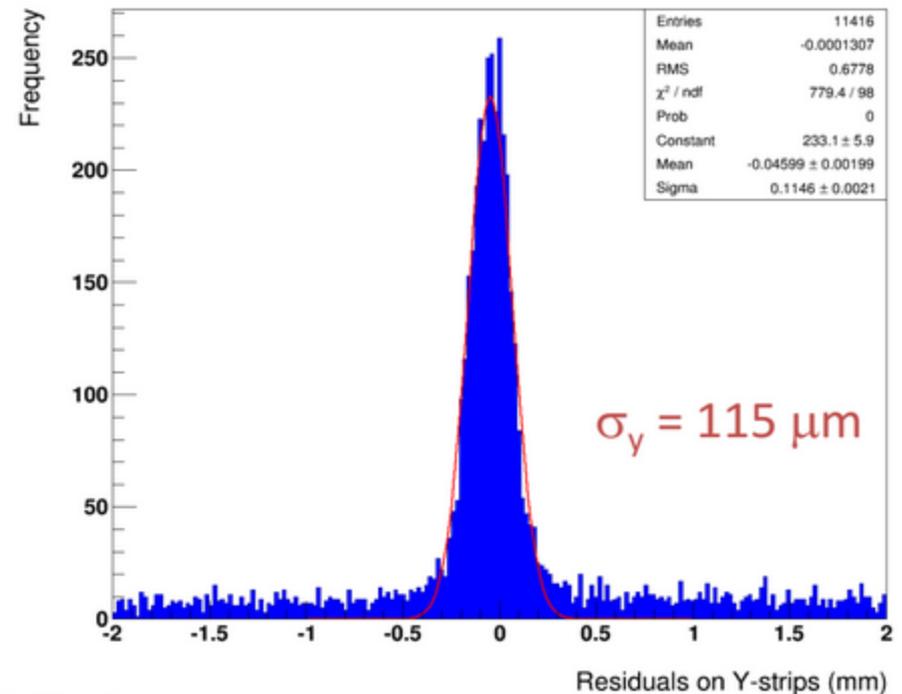


Now with the **correct** dimensions:

Large base: 430 mm, Stereo angle: 12.14°

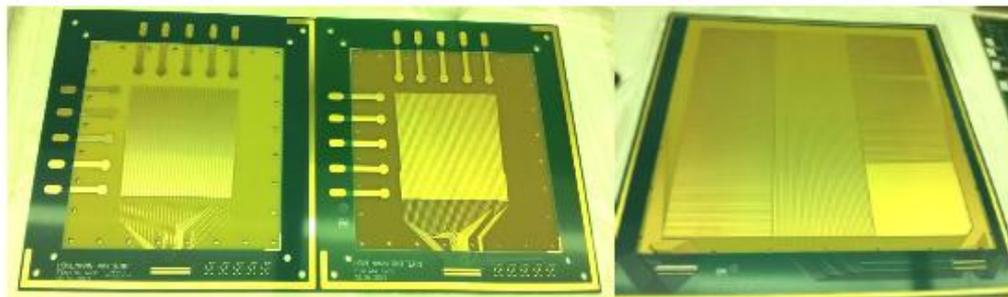
Double pic in Y residual distribution is gone

EIC1Y Residuals





Zig-Zags (aka Chevrons)



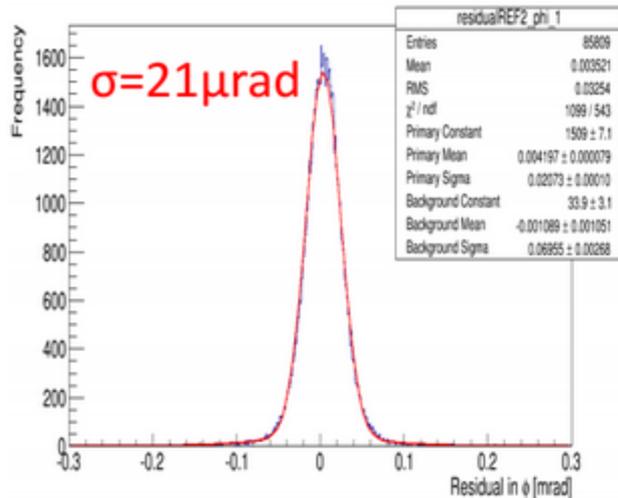
- ❑ Various patterns measured with cosmics in small chambers lead eventually to single choice for wedge chamber.

- ❑ HUGE savings in channel count.
- ❑ High resol. Only in bend direction, coarse in η .

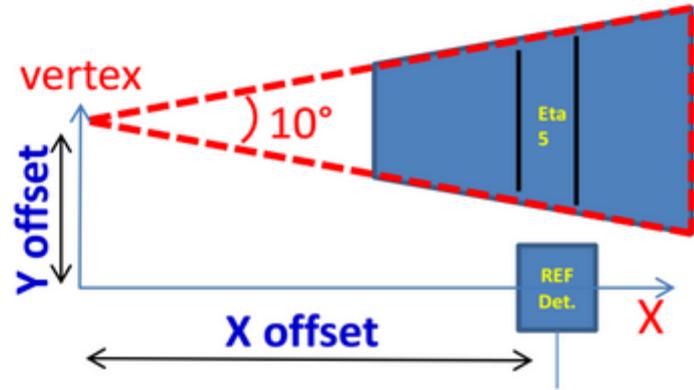
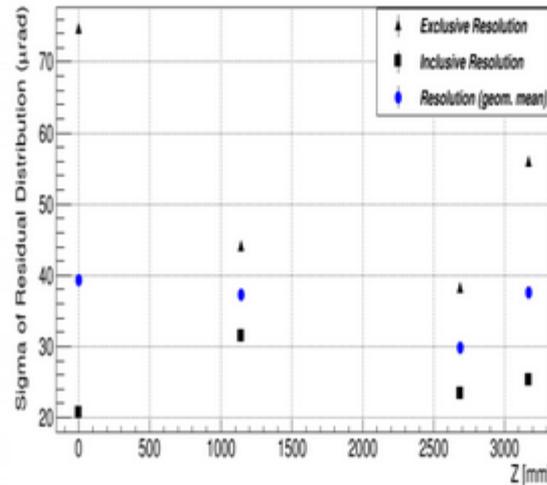


Tracking method for the zigzag GEM detector

Inclusive residual for 1st tracker



Resolution in φ for trackers

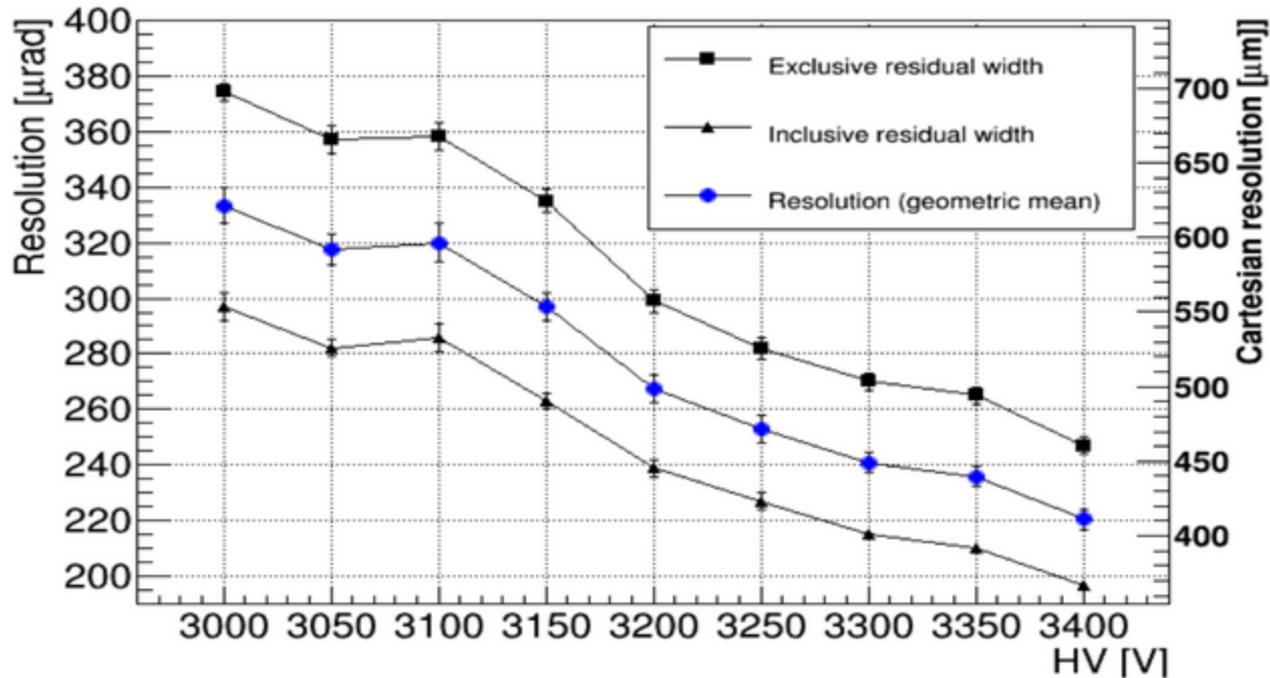


- After aligning the trackers to each other with shifts and rotations, they are giving resolutions around **70 μm** (the typical spatial resolution for GEM detectors) in both X and Y.
- The radial zigzag strips have a pitch of 1.37mrad, so we study the resolution in its natural **polar coordinate (φ)**.
- Tracking in polar system was demonstrated to be working as well as in Cartesian system. The trackers have azimuthal resolutions around **30 μrad** .
- The φ resolution of the zigzag GEM detector can be studied if its vertex is taken as the origin of the tracking system. **(X,Y) offsets** need to be optimized for the trackers to match that origin.



Spatial resolution results for the zigzag GEM detector

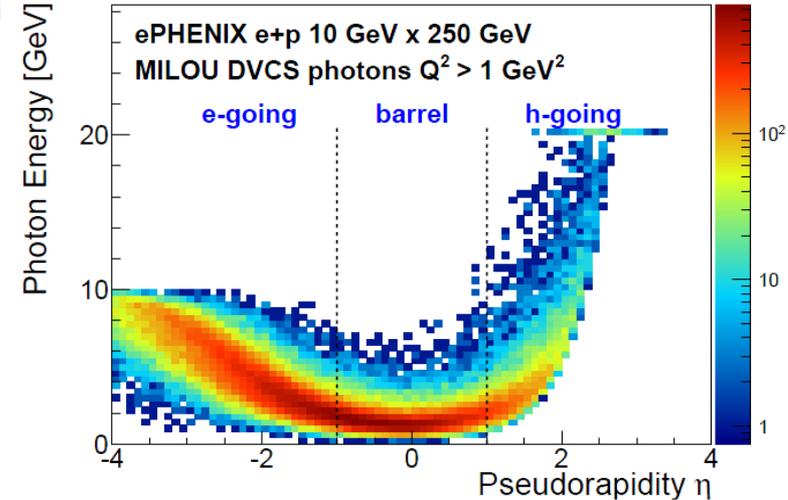
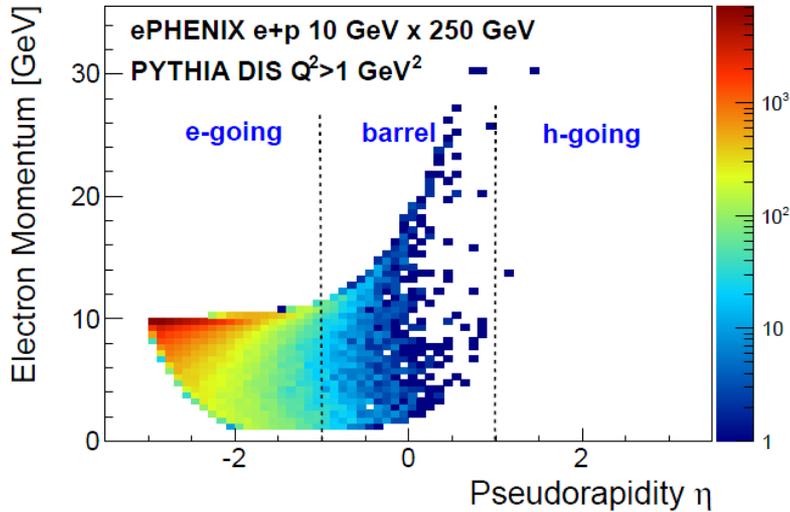
Resolution vs. HV in middle-sector 5



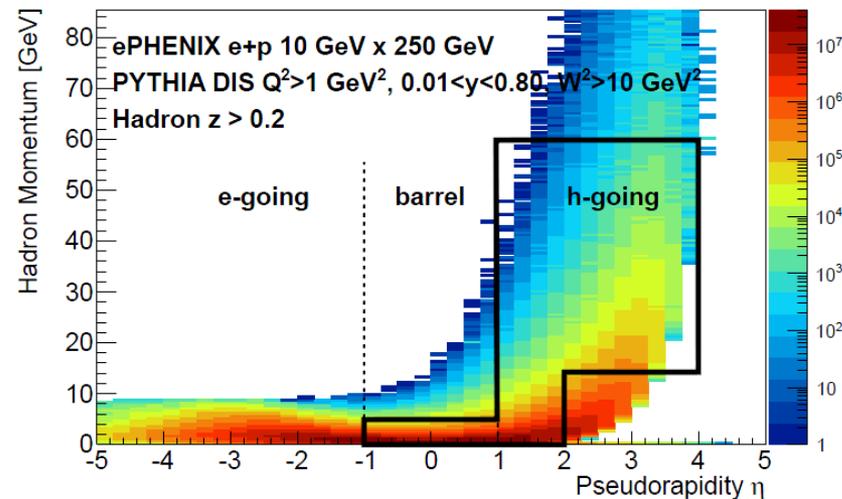
- The resolution of the detector is calculated as the geometric mean of the exclusive and inclusive residual widths: $\sigma = \sqrt{\sigma_{ex} \times \sigma_{in}}$
- Resolution @ 3300V is **(241±3)μrad** (17.6% of strip pitch), which corresponds to **(449±6)μm** at R=1866mm.



Measure what comes out!



- ❑ ep (eA) **HIGHLY** asymmetric.
- ❑ Moderate momenta for **ALL** species mid- and negative- η .
- ❑ At mid-rapidity principally low momentum:
 - **dE/dx** at lowest p.
 - **DIRC** to extend to **$\sim 8 \text{ GeV}$**
- ❑ Fwd η **BIG** challenge
 - **Hadron ID req'd to $60 \text{ GeV}/c!!$**



Ring Imaging Cherenkov is only known technology with required momentum reach!



Compact RICH? Impossible!



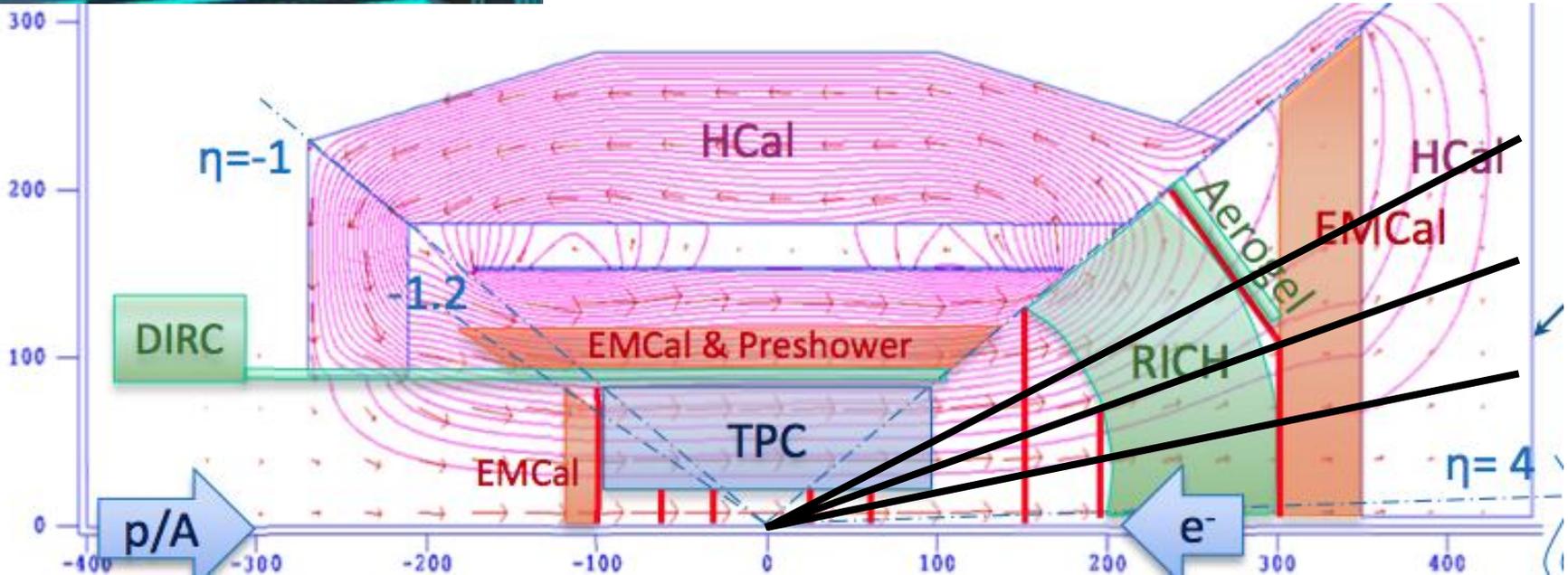
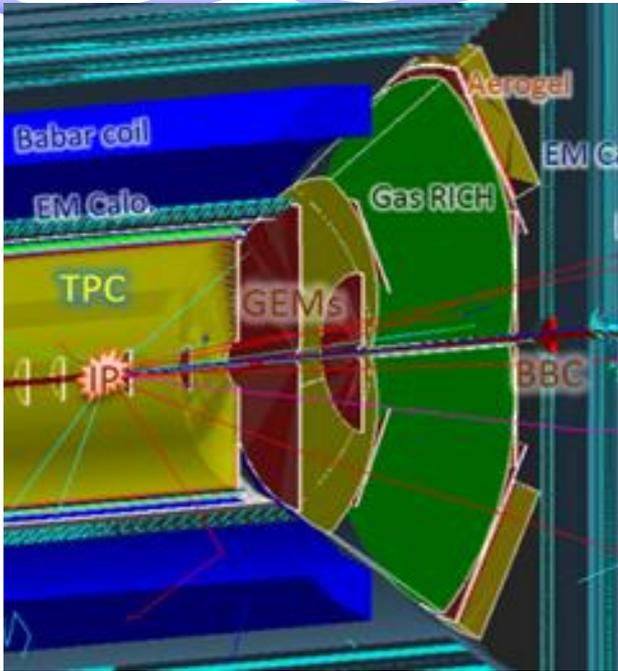
- ❑ LHCb required 3 meters of radiator (each) for C₄F₁₀ AND CF₄. At 4.5 meters, you hit the accelerator!
- ❑ If the RICH is small it is close to the interaction.
- ❑ There will be B-field in the RICH, bending smears rings!
- ❑ The B-field will kill PMTs and m² of SiPM breaks the bank.
- ❑ Single photons are tough.
- ❑ LHCb (and PHENIX) direct focused light to the side. You have no room, hermiticity lost!
- ❑ How can you measure rings for particle near beam pipe?

- ❑ We've budgeted one meter for the radiator a RICH that can perform Kaon ID to 60 GeV/c.
- ❑ Indeed.
- ❑ Our field will not bend tracks while inside the RICH.
- ❑ We have a cheap tech to cover m² areas at low cost.
- ❑ Our tech can handle it.
- ❑ Our tech is thin enough for the particle beam to go directly through the sensors.
- ❑ Clever Optics.



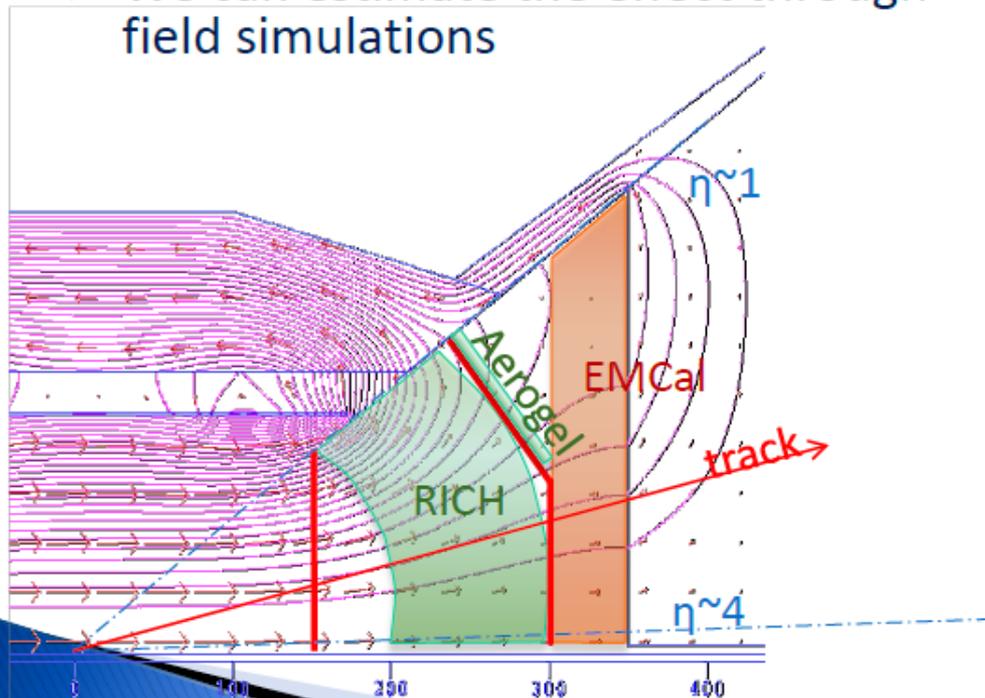
RICH drives Magnetic Field Shape

- The RICH will necessarily be tucked close to the solenoid.
- There will necessarily be field.
- Since we cannot set $\vec{B} = 0$, we instead approximate $\vec{v} \times \vec{B} = 0$ using shaped field lines:



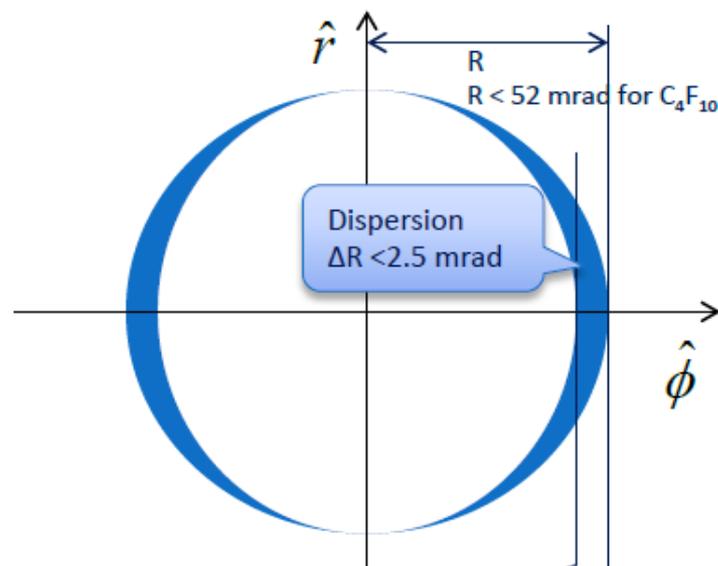
Field effect - distortion for RICH

- ▶ Field calculated numerically with field return
- ▶ Field lines mostly parallel to tracks in the RICH volume with the yoke
- ▶ We can estimate the effect through field simulations

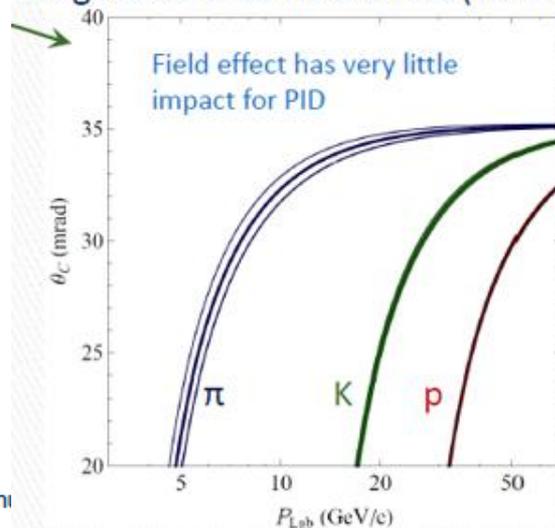


A RICH Ring:

Photon distribution due to tracking bending only

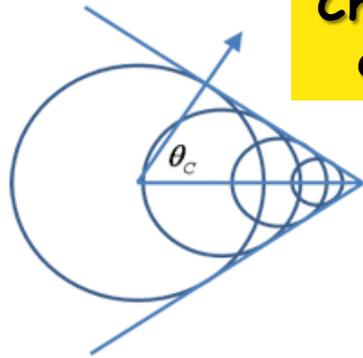


Ring radius $\pm 1\sigma$ field effect (for worst $\eta=1$)



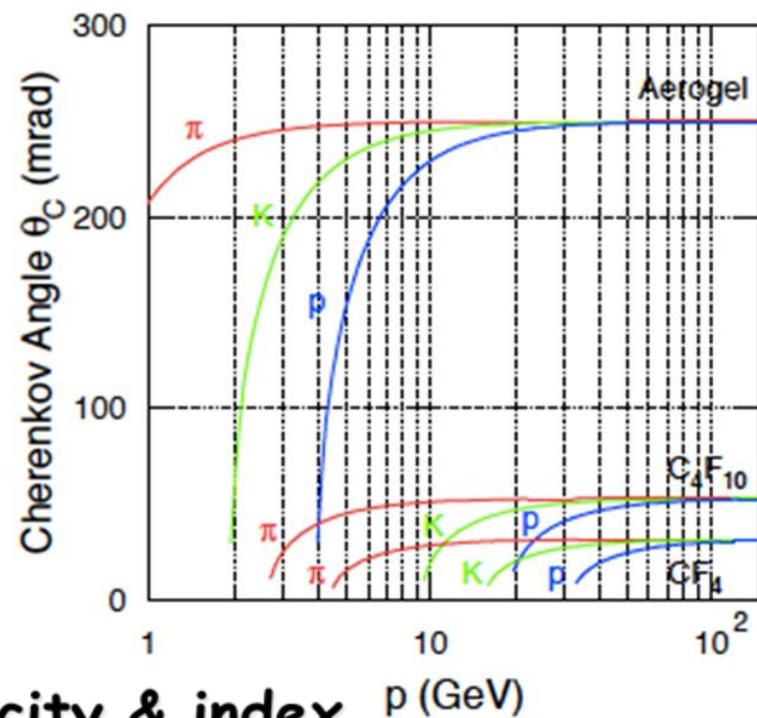


Cherenkov Light



Cherenkov Angle determines β

$$\theta_c = \cos^{-1} \left(\frac{1}{\beta n} \right)$$



❑ Cherenkov Light - “Optical Boom”

❑ Cherenkov angle depends upon velocity & index

- Low n distinguishes particles to high momentum.
- Low n yields less light!

❑ Go where the light is:

$$\text{➤ } \frac{dN}{dL} = 2\pi\alpha_{EM} \sin^2 \theta_c \int_{\lambda_{MIN}}^{\infty} \varepsilon(\lambda) QE(\lambda) \frac{1}{\lambda^2} d\lambda$$

➤ Deep UV Cherenkov yield is highest...how to get there?

➤ PHENIX HBD: No Optics allows for VERY low λ_{min}

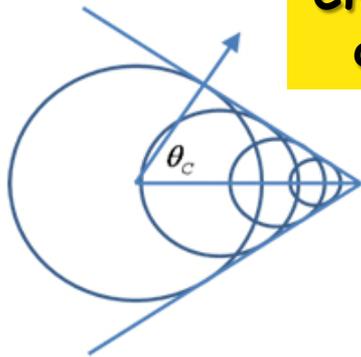
➤ But a RICH requires optics! What to do?



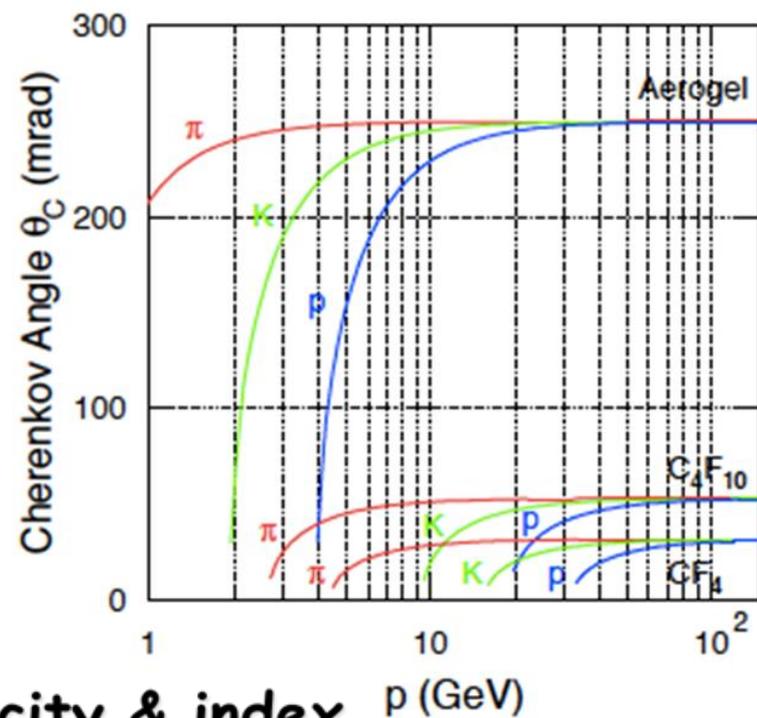


Cherenkov Light

Cherenkov Angle determines β



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- $\frac{dN}{dL} = 2\pi\alpha_{EM} \sin^2 \theta_C \int_{\lambda_{MIN}}^{\infty} \epsilon(\lambda) QE(\lambda) \frac{1}{\lambda^2} d\lambda$
- Deep UV Cherenkov yield is highest...how to get there?

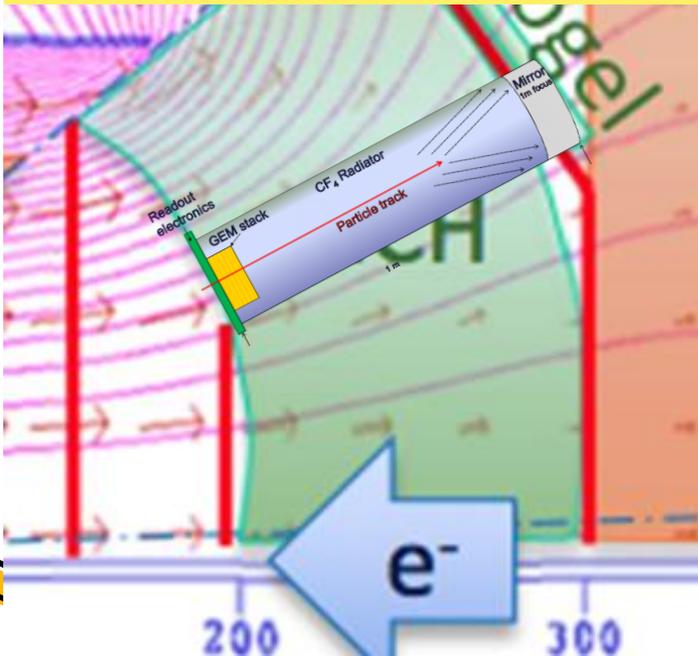




Outline of Requirements



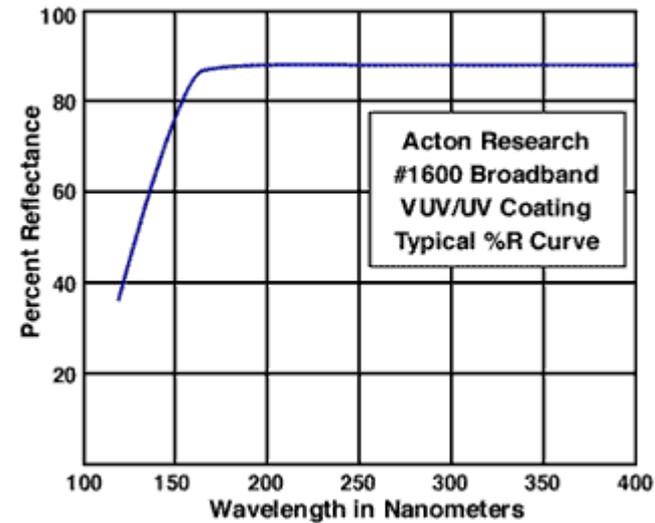
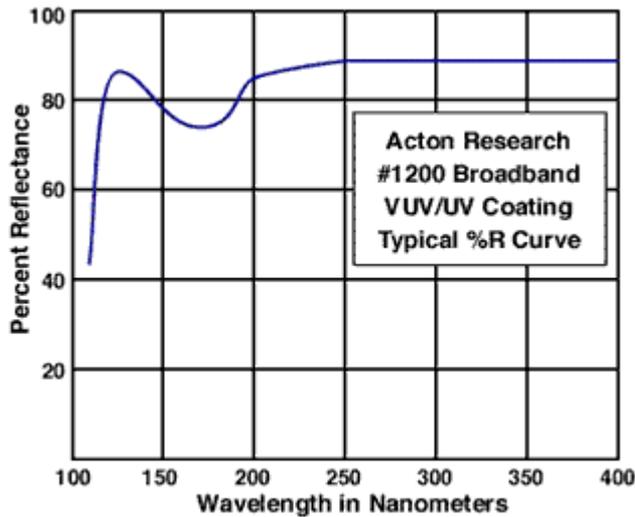
| Requirement | Technology | Status |
|--|------------------------------------|----------------------|
| Low index gas w/ high light yield by UV transparency | CF ₄ | Achieved: PHENIX HBD |
| Photon Detectors in Field | Photo-sensitive GEM | Achieved: PHENIX HBD |
| m ² focal plane coverage | Photo-sensitive GEM | Achieved: PHENIX HBD |
| Hermetic Acceptance | Particles pass through focal plane | Achieved: PHENIX HBD |
| Single photon detection | Gain 10 ⁵ or higher | R&D |
| DEEP UV Optics | Dielectric Film Mirror | R&D |



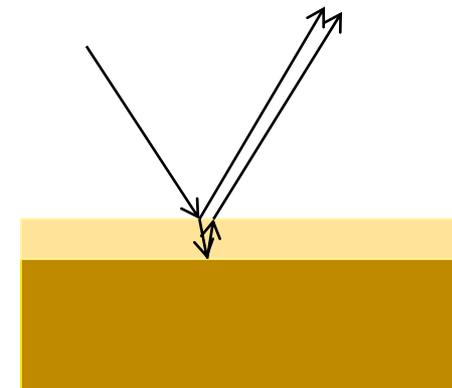
- R&D to develop small prototype
- 1 meter radiator
- Photo-sensitive GEM readout
- Test Beams:
 - SLAC May/June 2013
 - **FNAL October 2013**



Commercial (small) mirror Reflectivities



- ❑ Bare aluminum mirrors no good (AlO...high cutoff).
- ❑ Better has MgF_2 overcoat (right hand).
 - Exists and has been made to large scale.
 - Not good enough.
- ❑ Thin Film Interference!
 - Tuned for peak at 120 nm.
 - Retrieves (most of) the lost light.

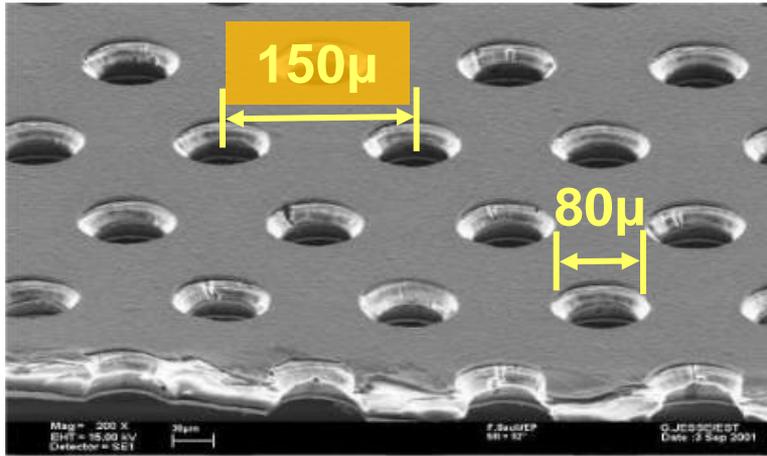


Thin Film Interference



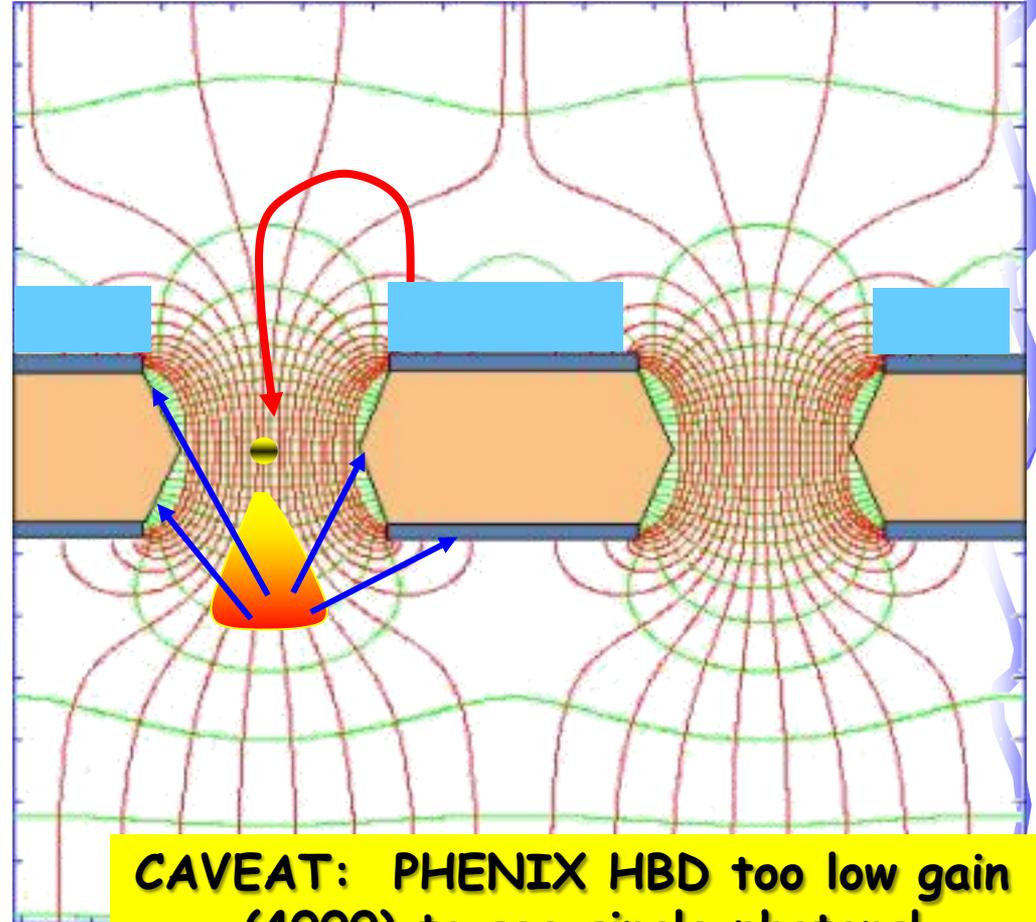


Gas Electron Multiplier for PHOTONS!



- ❑ The original idea by F.Sauli (mid 90s) US Patent 6,011,265
- ❑ Traditionally CHARGED PARTICLE detectors (not photons)

- ❑ Two copper layers separated by insulating film with regular pitch of holes.
- ❑ HV creates very strong field such that the avalanche develops inside the holes
- ❑ Just add the photocathode
- ❑ By the way: no photon feedback onto photocathode

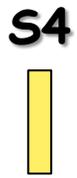
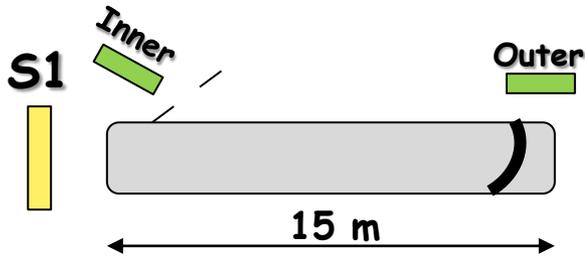


CAVEAT: PHENIX HBD too low gain (4000) to see single photons!

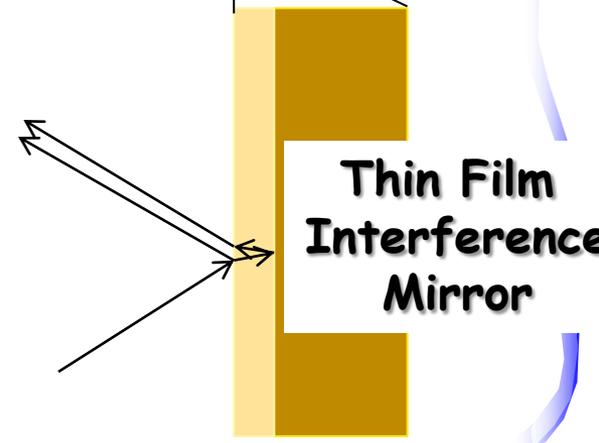
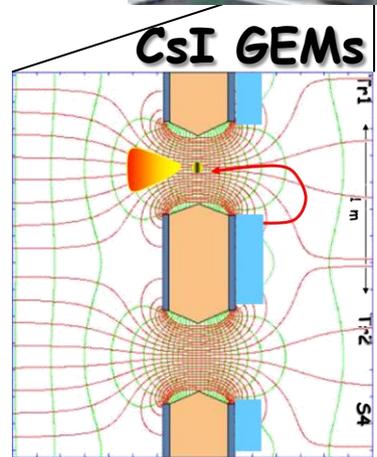




MT6 2D: RICH Detector

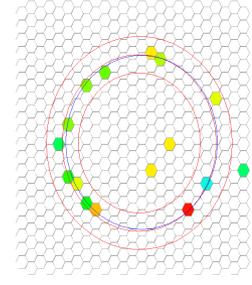
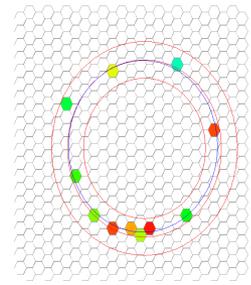
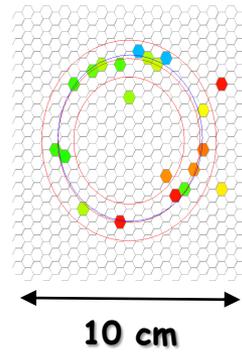


- Beamline Cerenkov
- PID offline
- K-Trigger



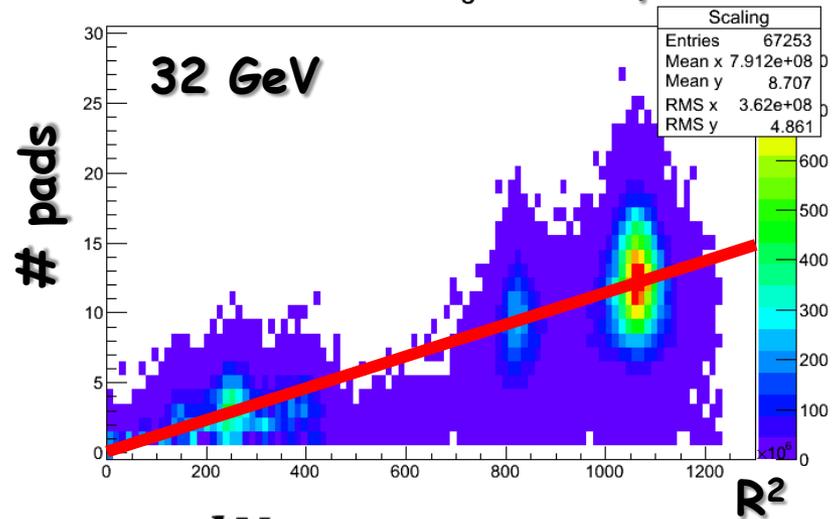
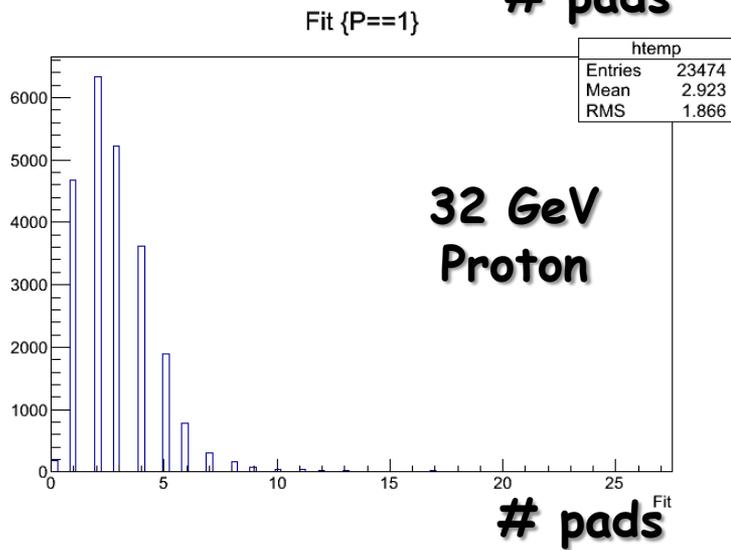
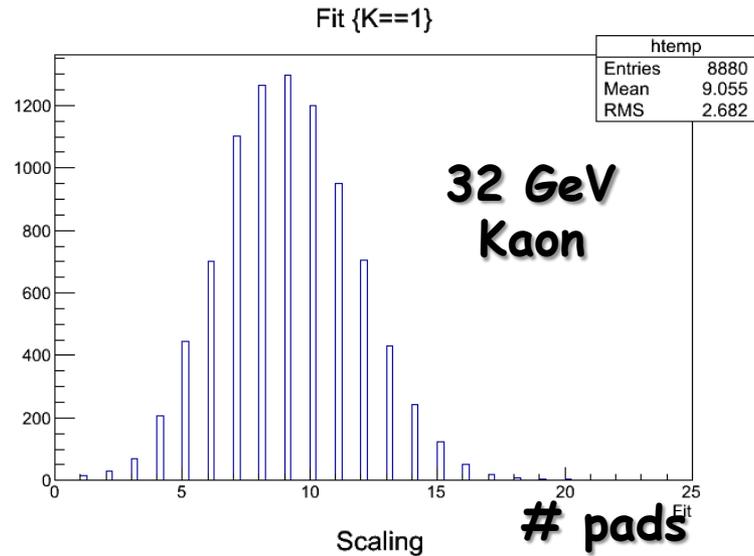
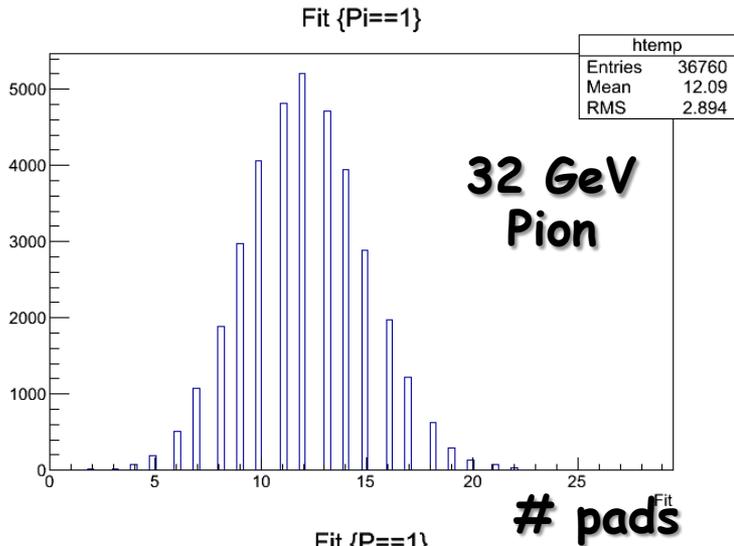
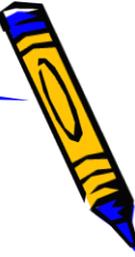
- Goal: PID to 60 GeV/c
- Rings in only 1 meter of gas
 - LHCb uses 3 meters

- Technique:
 - Deep UV mirror
 - CsI GEMs





Number of Pads Included in the Fit:

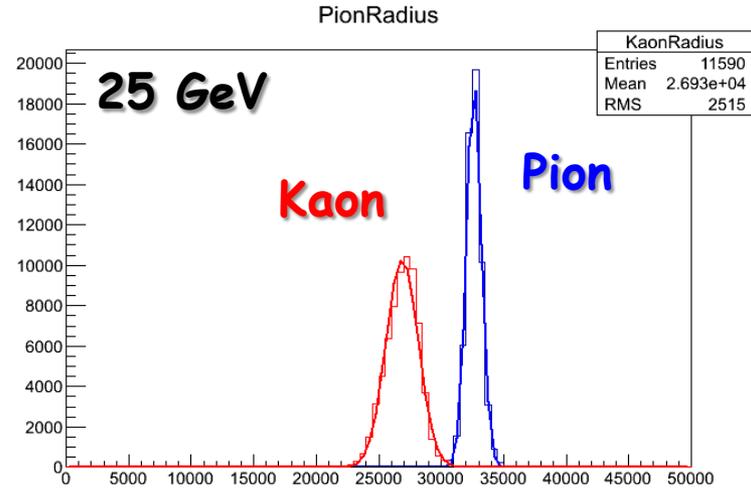
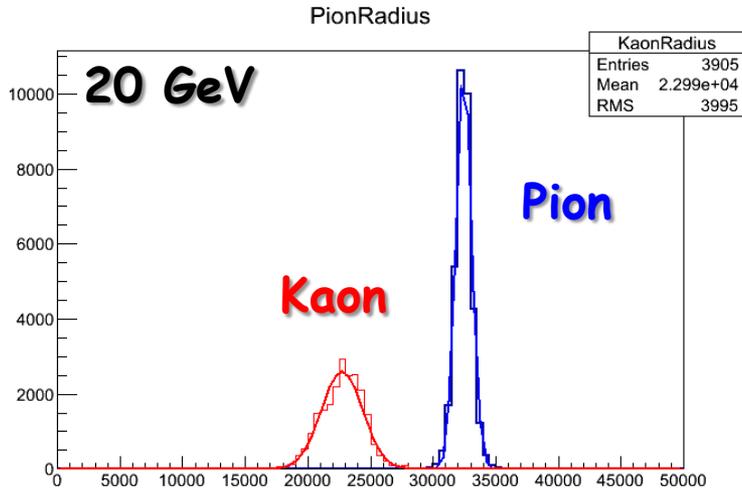


□
$$\frac{dN_\gamma}{dL} \approx \sin^2 \theta_c \approx R^2$$

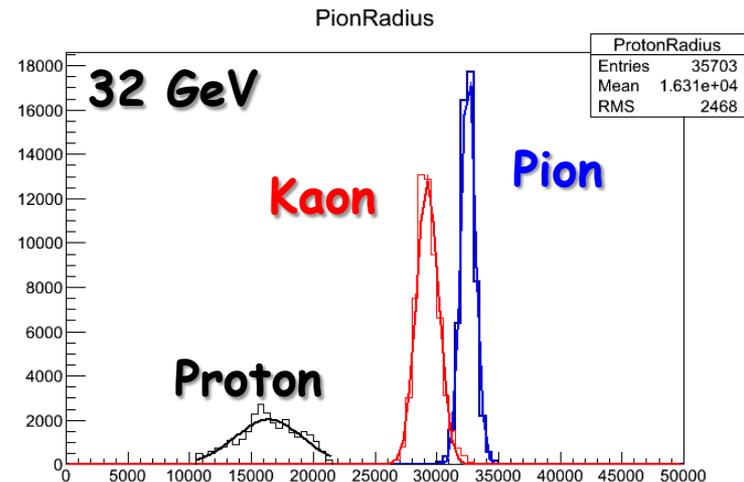




Radii Results:



- Reasonable results at all measured energies.
- NOTE: 32 GeV is the highest available energy for Kaons at FTBF.

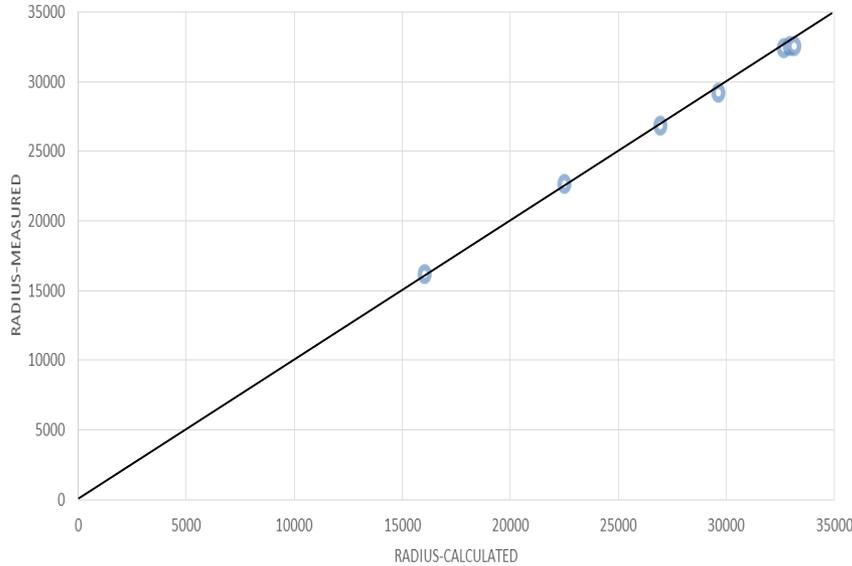




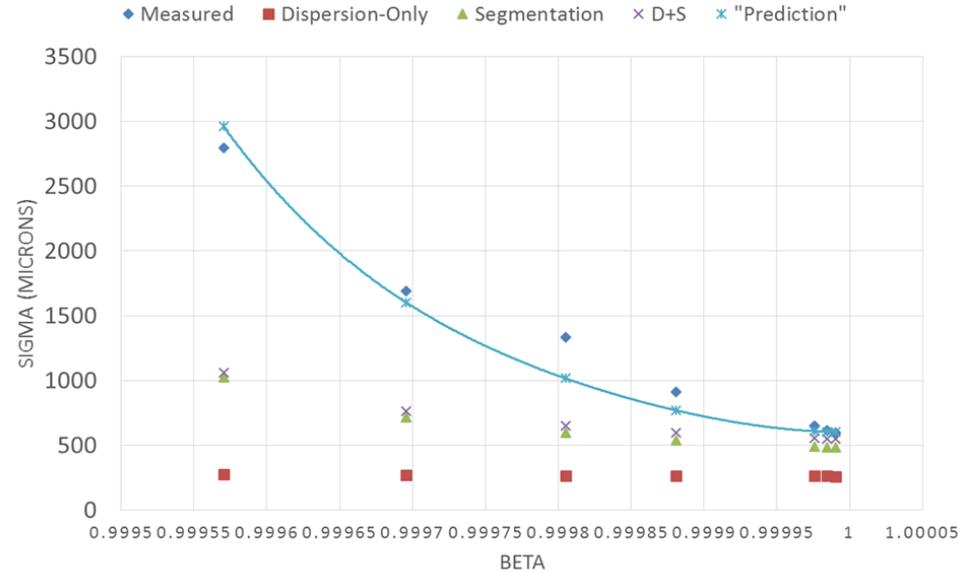
Radius & Width Matches Expectation.



Radius Expectation



RING WIDTHS



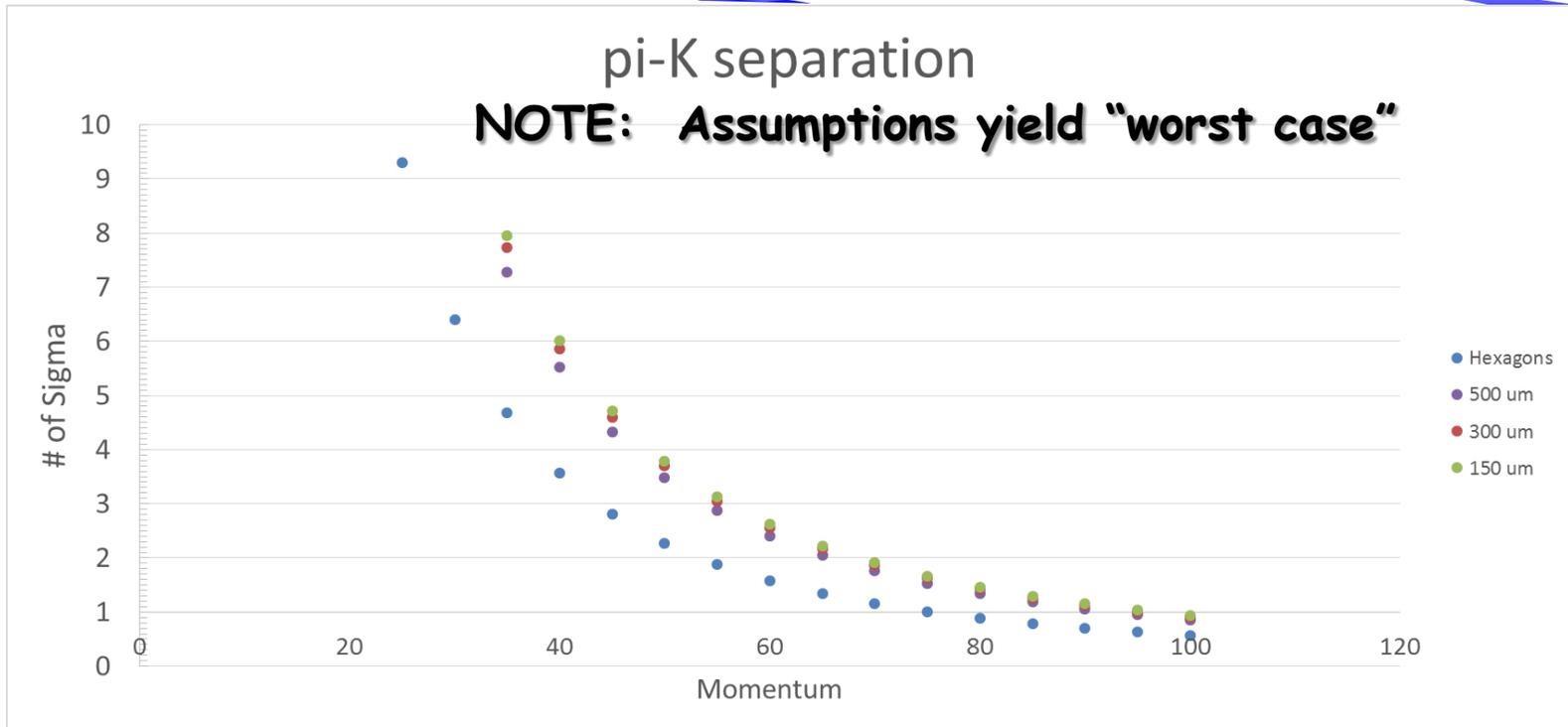
- ❑ Index = free parameter.
- ❑ $n = 1.000558$
- ❑ n matches literature.

- ❑ Influenced by momentum spread delivered in beam.
- ❑ Assume $\frac{\delta p}{p} = const.$
- ❑ Fit $\frac{\delta p}{p} = 5\%$ (reasonable)





PID to 60 GeV w/ better position resolution



- ❑ Dispersion eventually becomes limiting factor.
- ❑ 500 micron (sigma) photon position resolution is easy goal.
 - Hence proposed R&D for Resistive Charge Division.
- ❑ ~2.5 sigma separation at 60 GeV!





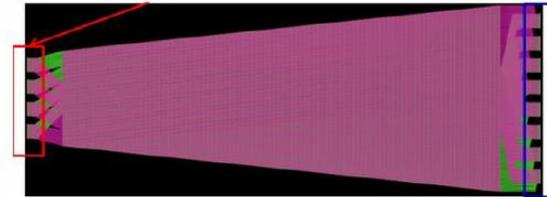
Next Steps: Core Research



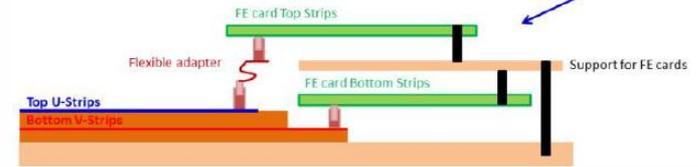
Core Tracking:

- Move stereo readouts away from beam pipe.
- Complete & Test TPC/HBD Concept
- Improved uniformity of response for zig-zag chamber and improved test station.
- **\$251k**

Remove the contacts at the bottom of the GEM → Avoid the FE card in hard radiation dose area



Concentrate all the contacts on the top of the GEM with a high density FE cards connectors thanks to the new idea described below



Core Mirror:

- Refurbish Big Mac vacuum chamber to become evaporator.
 - @ Postponed as lower priority to deal with budget profile.
- **\$83k**

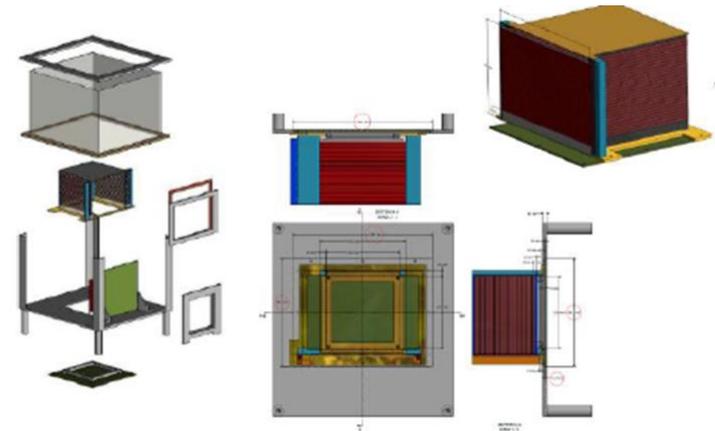


Figure 6 3D model of the prototype TPC/ Cherenkov detector.





Next Steps: New Ideas

□ Hybrid Gain Stages GEM+MMG

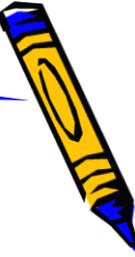
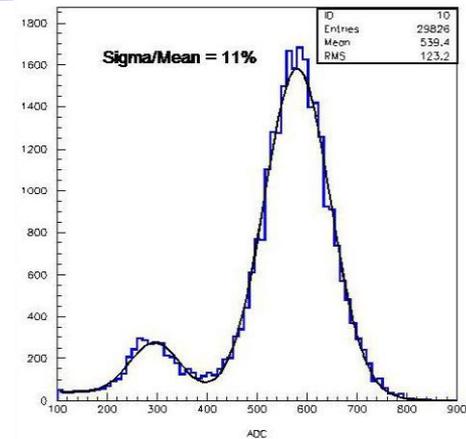
- Very low ion feedback
- Peaked single-*e* response
- **\$35k**

□ Resistive Charge Division

- Avalanche spot in RICH has $\sigma=132 \mu\text{m}$.
- Cannot use geometrical charge division.
- Alternative to high channel count is resistive division.
- **\$10k**

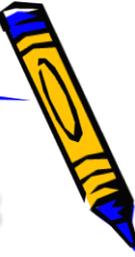
□ Central Barrel Tracking TPC

- TPC/HBD is most useful for 2nd phase EIC.
- Fast TPC necessary for 1st phase in most designs.
- New Collaborators to pursue new research.
- **\$100k** (to be defended in May/June).





Summary



- ❑ The EIC Tracking/PID Consortium has completed our sector test for forward tracking & RICH in October 2013 (**ahead of schedule**).
- ❑ Results are uniformly excellent; at or near EIC specs.
- ❑ Hemmick believes this is among the most productive R&D efforts he has witnessed in his career.
- ❑ Consortium funding “per institution” very cost effective.
- ❑ FY14 Outlook (not including salaries).
 - Core Tracking: \$251k
 - Core Mirror: \$83k
 - New Hybrid Gain: \$35k
 - New Resistive Div: \$10k
 - New TPC (May/June): \$100k

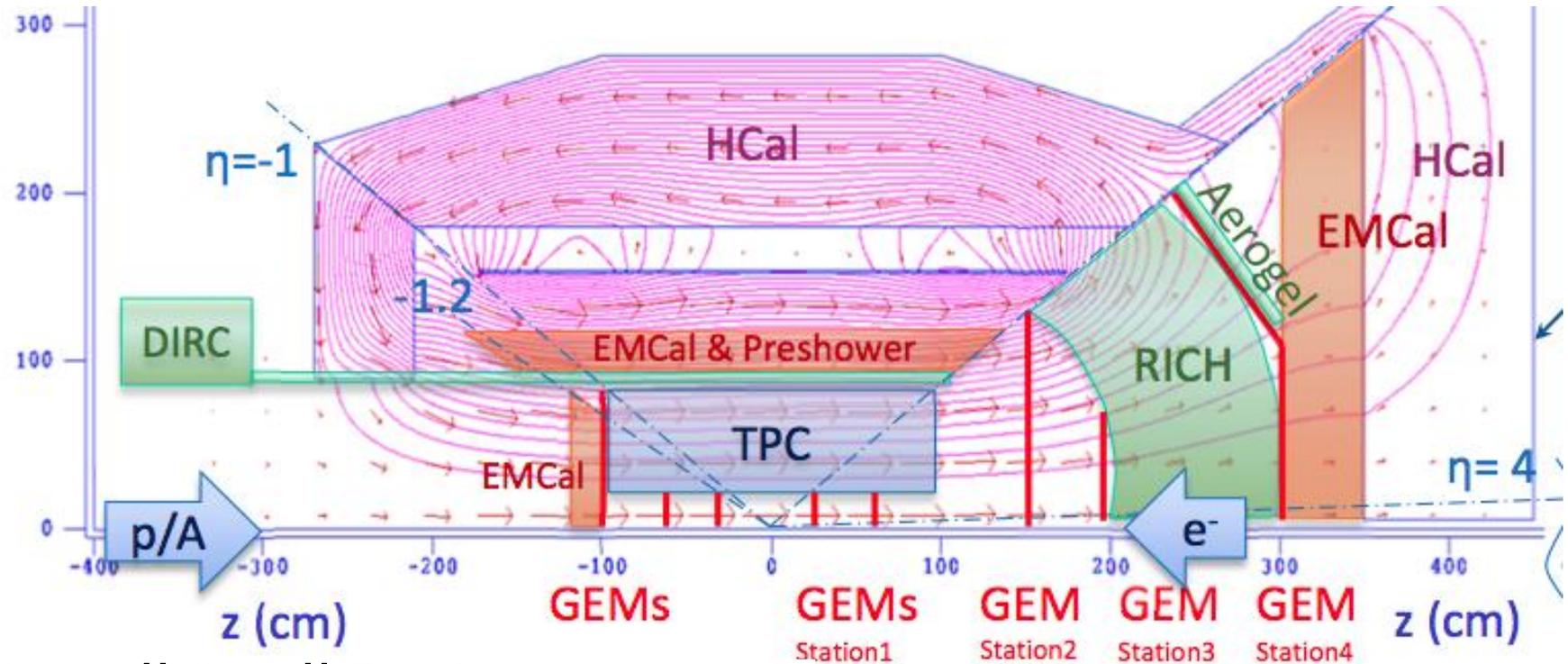


Backups...

Summary

- ▶ TPC provides PID, low mass, hermetic tracking.
- ▶ TPC is principle choice of most EIC designs.
- ▶ ALL EIC designs require RICH which constrains TPC to be small/compact device.
- ▶ Fast/low diffusion gas for Au+Au.
- ▶ Likely wish un-gated:
 - Quad-GEM or mixed mode GEM/ μ MEGA.
 - Follow ALICE upgrade plans?
- ▶ Electronics:
 - Follow ALICE upgrade plans? (Anders Oskarsson)

TPC Constraint Summary:



- ▶ Overall Small Device:
 - B-field “Sweet Spot”
- ▶ Outer radius:
 - Driven by BaBar DIRC → < 80 cm
- ▶ Length:
 - η -accept → ~2 meters full length.
- ▶ Inner radius:
 - Not tightly constrained
 - Leave room for Silicon?
- ▶ Resolution
 - eA not challenging.
 - AuAu Y(1s), Y(2s), Y(3s) is doable (I. Ravinovich/B. Selihan)
- ▶ Gating(?)
 - ~ 10kHz for $Q^2 > 1 \text{ GeV}^2$
 - Likely want un-gated solution.



"Full Disclosure"



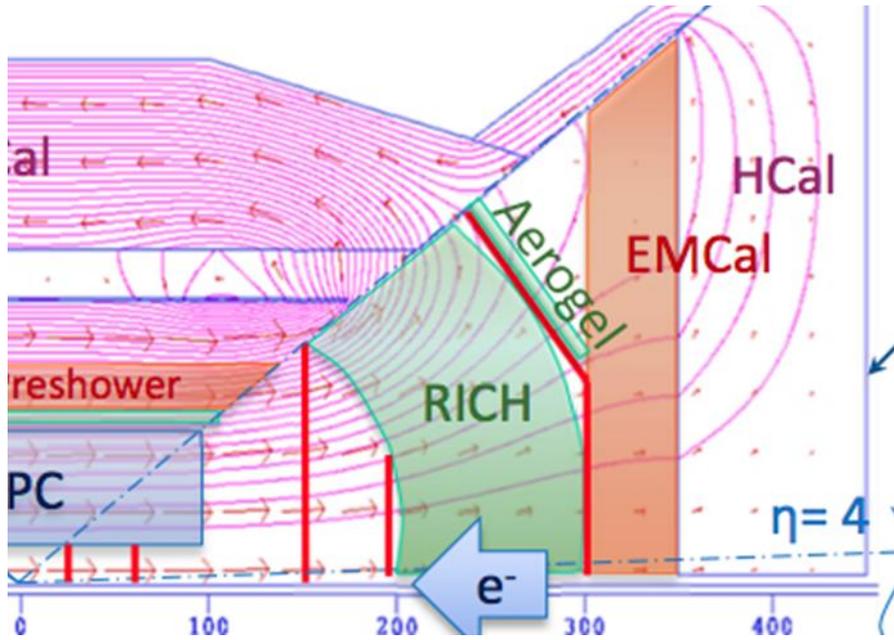
| Item | Comment | Total |
|--------------------|--|--------|
| Salaries | Must be Fully Funded. Top Priority Includes \$180k of EIC-wide Simulation Effort | \$269k |
| Core: Tracking | Lean @ 75%; Dead at 50%. | \$251k |
| Core: Mirrors | Approved June 2013, Can be postponed. | \$83k |
| New: Hybrid Gain | Lean Proposal. Requires full funds to execute. | \$35k |
| New: Resistive Div | Lean Proposal. Requires full funds to execute. | \$10k |
| New: TPC | Placeholder. New colleagues. Full Prop. In May | \$100k |

- ALL** FY14 monies associated with our consortium.
 - Some already "allocated" (e.g. Salaries/Core-Mirrors).
- Urge committee to remember that these funds are distributed across 7 institutions.
- We believe our consortium is exceptionally productive.
- We believe our per-institution requests are minimal.

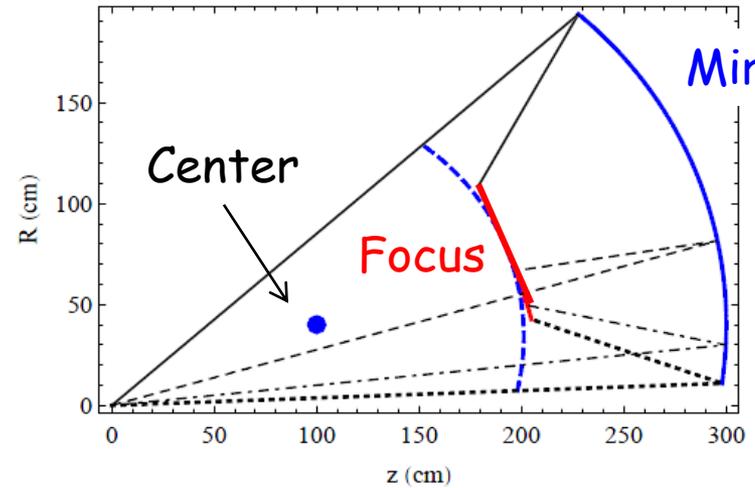




ePHENIX: Gas RICH



RICH Optics



- ❑ Magnetic Field in RICH!
- ❑ Field shaped to “point at collision vertex”.
- ❑ $\vec{v} \times \vec{B} \approx 0$.
- ❑ Not true near beam pipe!
 - OK, p is very large there.

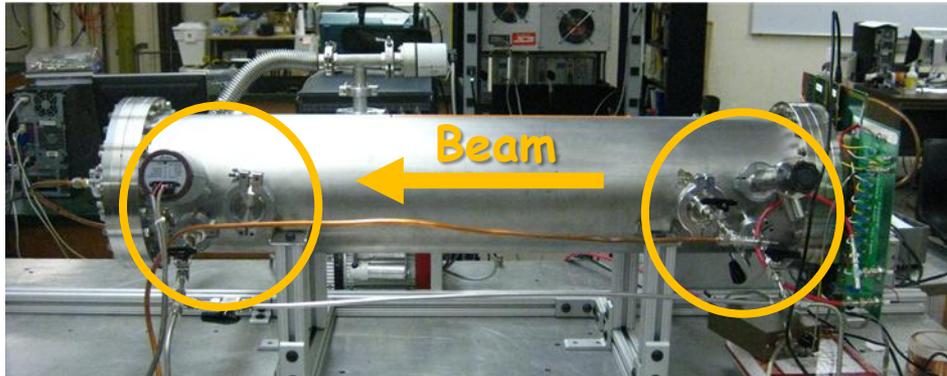
- ❑ Mirror(s) break symmetry.
 - Reduced focal plane size: no dead area at edge.
 - Improved acceptance for light from high η particles
 - 6 segments around phi





Detector Design

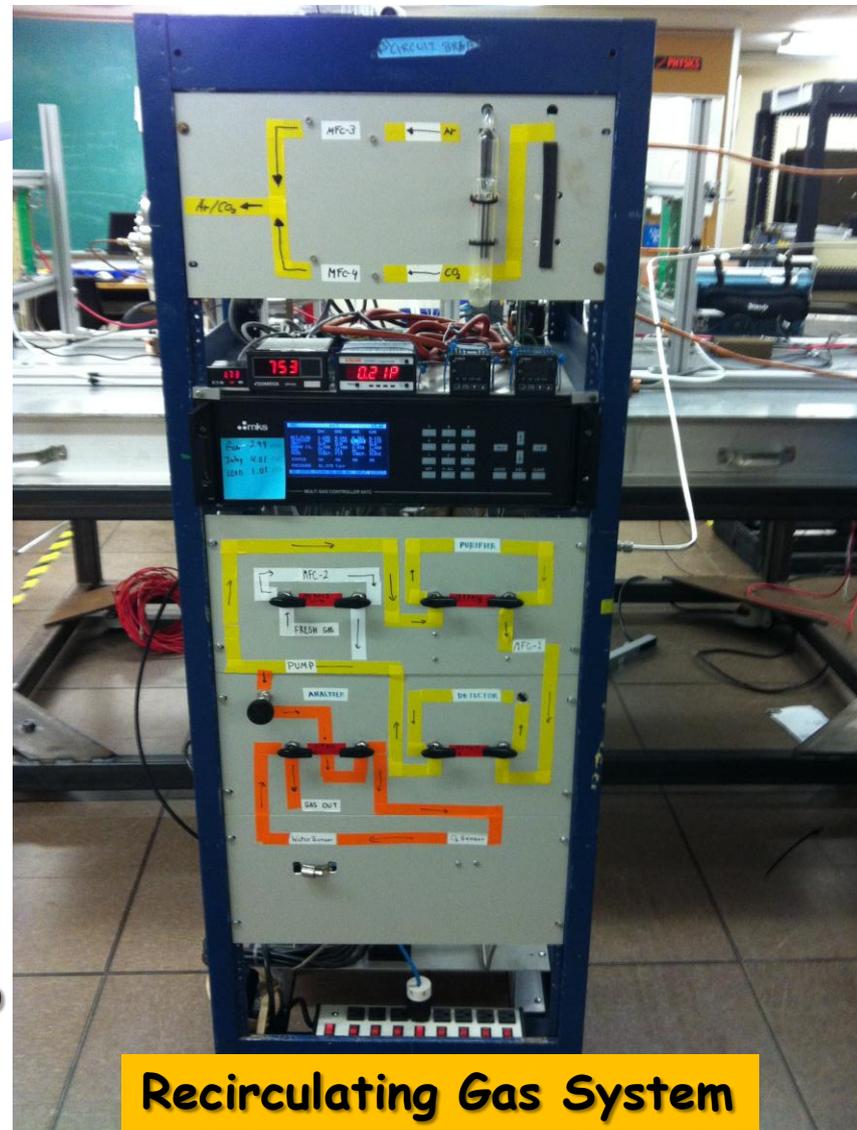
8" Conflat Flanges @ Ends



Clusters of KF Fittings



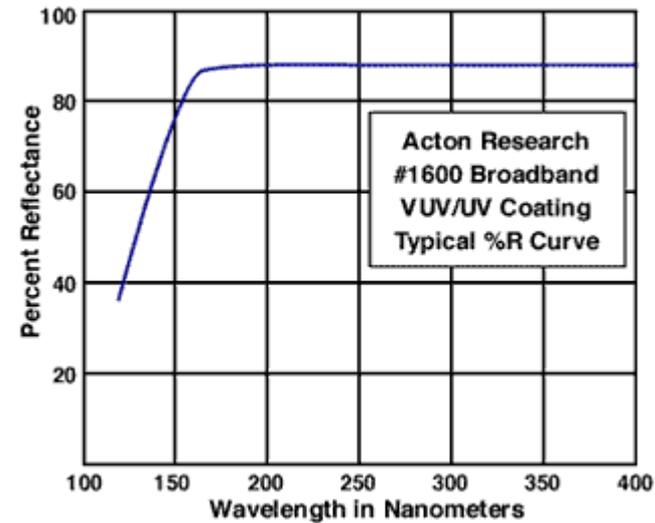
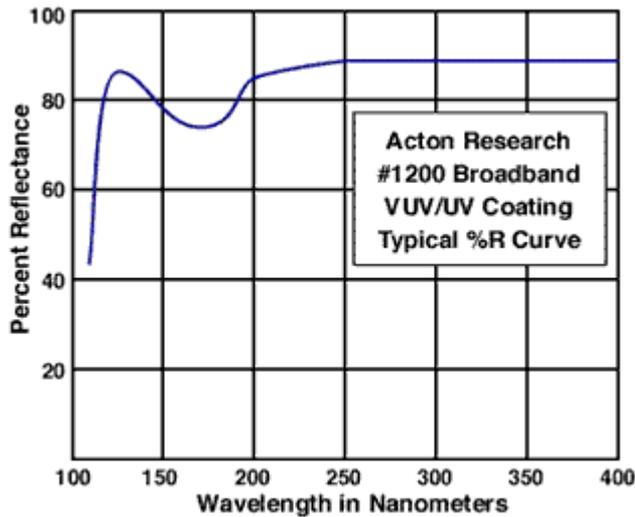
Molecular Drag Pump
Backed by Diaphragm Pump



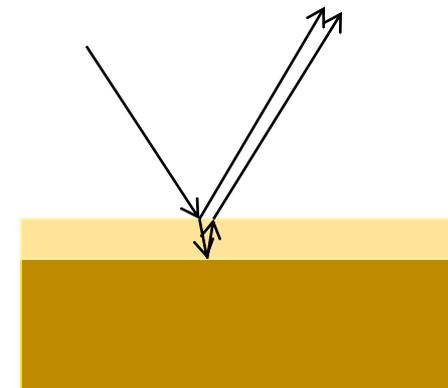
- ❑ All SS construction
- ❑ Commercial parts for EVERYTHING except GEM plane.



Commercial (small) mirror Reflectivities



- ❑ Bare aluminum mirrors no good (AlO...high cutoff).
- ❑ Better has MgF_2 overcoat (right hand).
 - Exists and has been made to large scale.
 - Not good enough.
- ❑ Thin Film Interference!
 - Tuned for peak at 120 nm.
 - Retrieves (most of) the lost light.



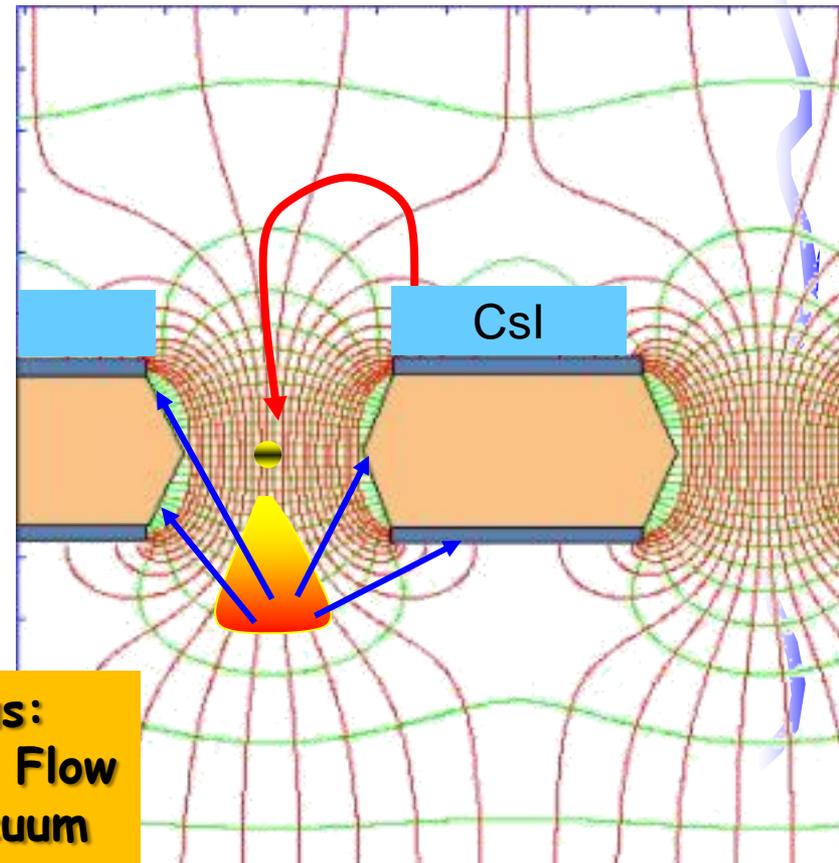
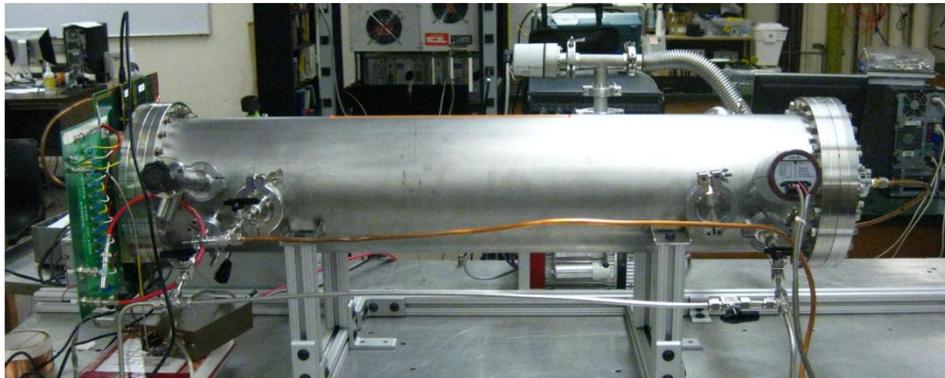
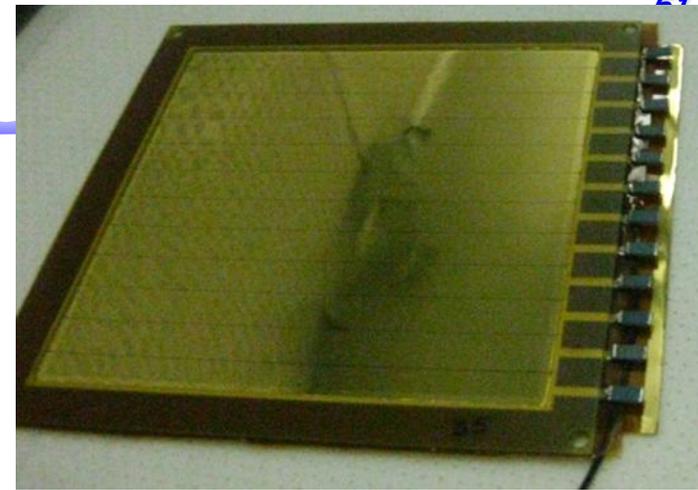
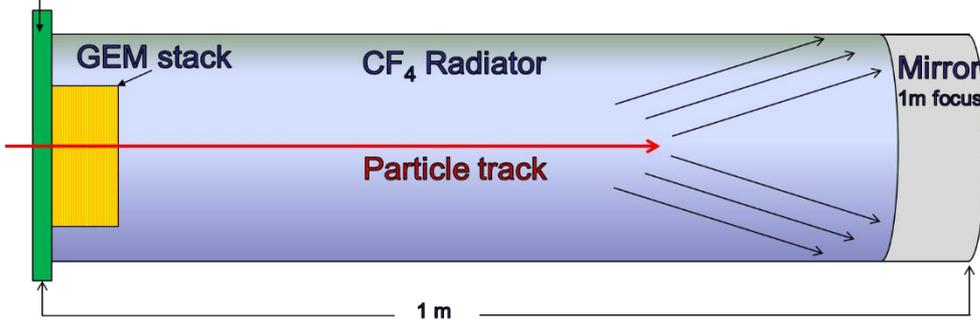
Thin Film Interference





Detector Overview

Readout electronics



- Spherical mirror makes ring:
 - Ring \rightarrow Cherenkov Angle
- Use photo-sensitive GEMs!
- Readout APV25 via SRS.

Detector dies when:

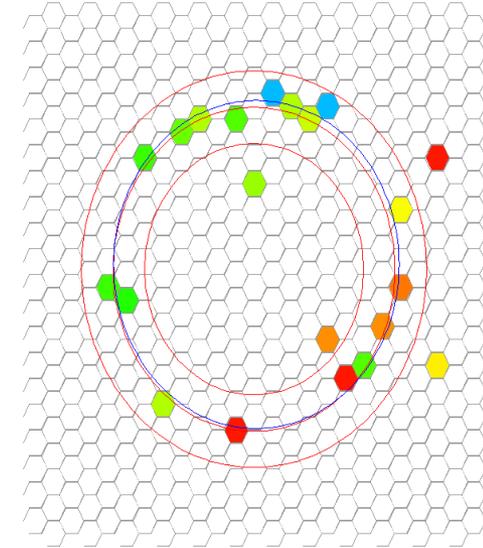
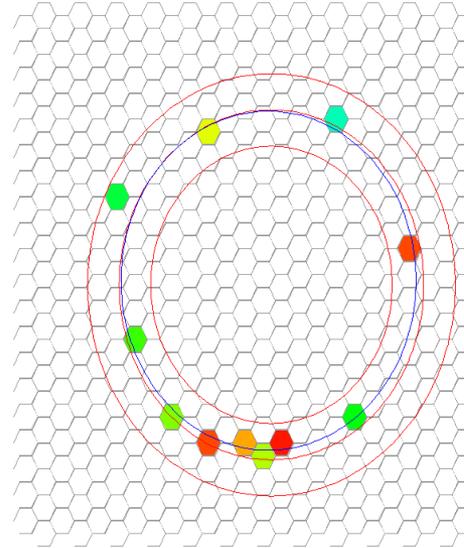
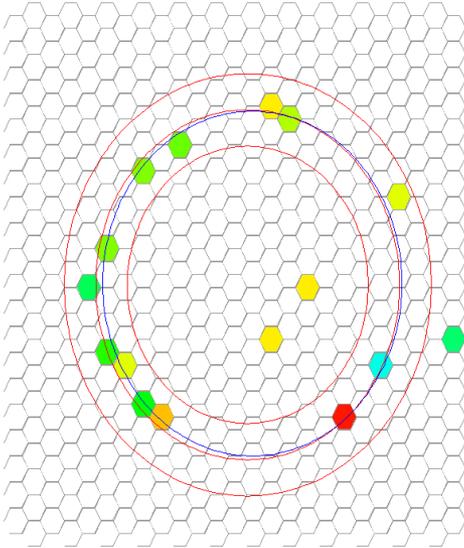
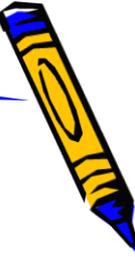
- Dust kills GEMs
- Water @ 20 ppm kills CsI

24-7 Status:

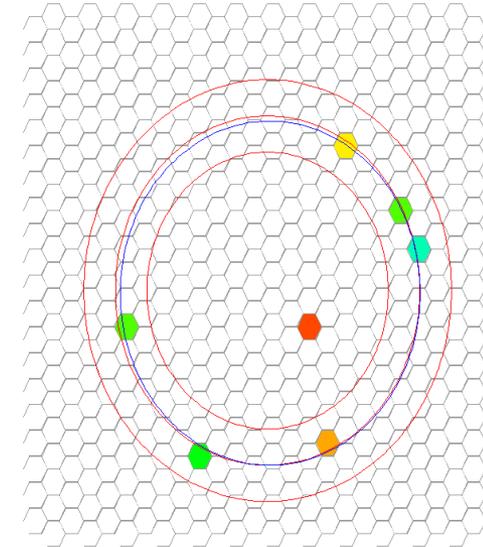
- UHP Gas Flow
- High Vacuum



Look at the "Hit" pads... See Rings!

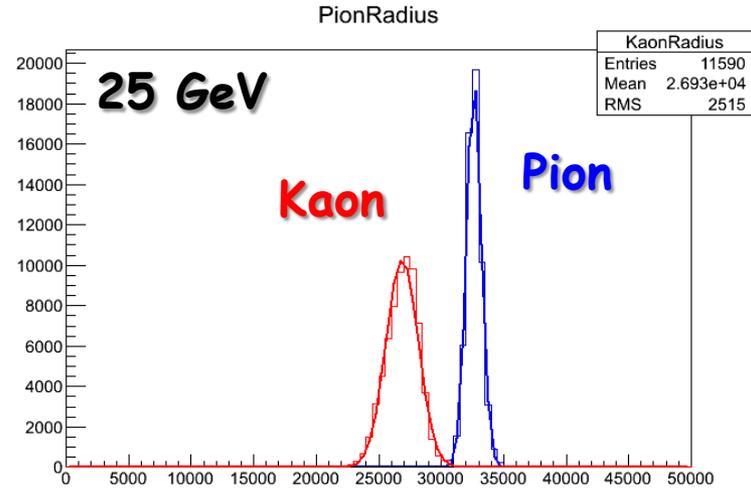
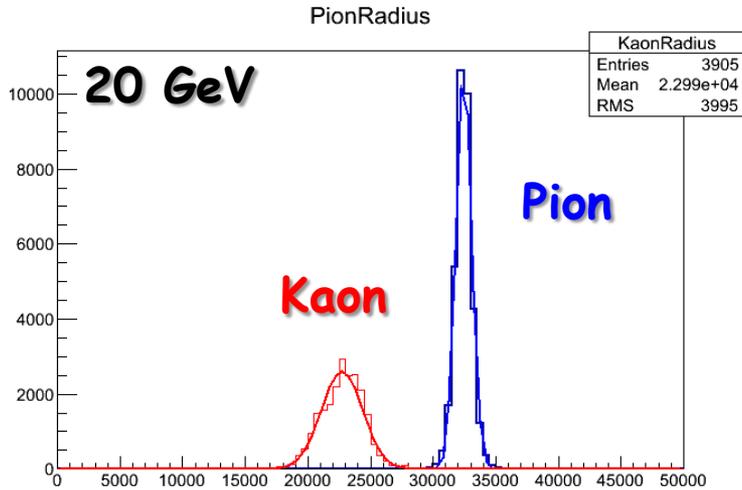


- ❑ Your eyes see the Rings very easily.
- ❑ **Red Circles: Pattern Recognition.**
- ❑ **Blue Circles: Robust Fit.**





Radii Results:



- Reasonable results at all measured energies.
- NOTE: 32 GeV is the highest available energy for Kaons at FTBF.

